

Note there is an Appendix with useful information attached to the back of the exam.  
Write all your calculations and answers in the exam book.

*Appendiks med nyttig informasjon er vedlagt på baksiden av eksamensoppgaven.  
Vis alle beregninger og svar i eksamensbesvarelsen.*

## I. SHORT ANSWER QUESTIONS - KORTSVARSOPPGAVER

(points for each question are shown as subscripts)

*(Poeng for hver oppgave er markert med senket skrift)*

A. <sub>6</sub> Briefly define Energy, Entropy and Exergy

*<sub>6</sub>Definer kort begrepene energi, entropi og eksergi.*

Energy is the ability to do work (kinetic + potential + mass) on an absolute scale

Entropy is a measure of the disorder of the system related to the number of possible configurations

Exergy is a measure of how far out of equilibrium *with the surroundings* that a system is, and represents the part of the energy that can be used to do work in a particular situation

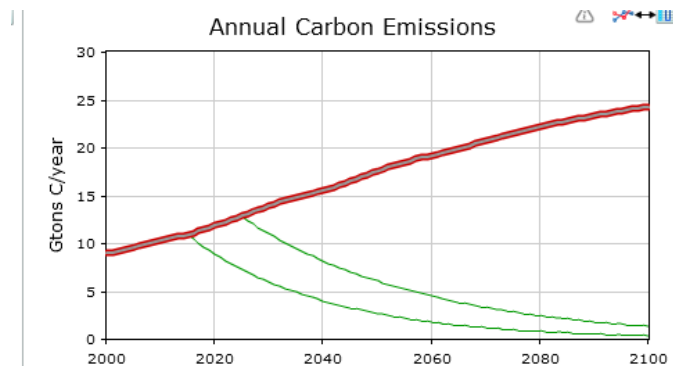
B. The graph below is from the EnRoads simulation used in the last day of class.

*Grafen under er fra EnRoads-simuleringen benyttet i siste forelesning.*

<sub>4</sub>What do the green lines represent?

*<sub>4</sub>Hva representerer de grønne linjene?*

The green lines are the bounds of CO<sub>2</sub> output allowable in the various models associated with a 2 °C increase in global temperature.



C. <sub>2</sub>What are the equivalents of the voltage and current when considering the case of thermal resistance of a building?

*<sub>2</sub>Hva tilsvarer spenning og strøm når en ser på termisk resistanse i en bygning?*

Voltage ~ temperature difference and current ~ heat flow

D. <sub>3</sub>Briefly explain two problems with the use of biofuels.

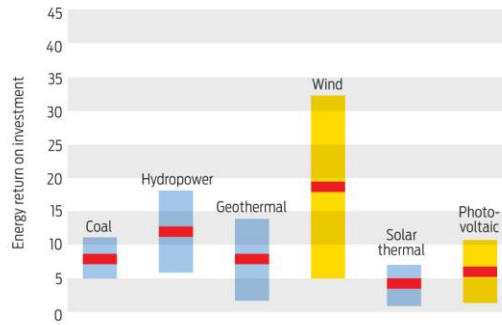
*<sub>3</sub>Beskriv kort to problemer med bruk av biodrivstoff.*

Competition between food and fuel crops, land use change release of greenhouse gases, low energy density

E. 5 Define EROI and rank two technologies from higher to lower value.

5 Definer EROI og ranger to teknologier fra høyest til lavest verdi.

Energy return on investment



F. 4 How can the latent heat of fusion be used as part of a household energy system?

4 Hvordan kan latent smeltevarme bli brukt som del av et husholdningsenergisystem?

Using a salt that melts/freezes near a comfortable room temperature stabilizes the temperature of a thermal mass in a passive solar system, e.g. Glauber's salt.

G. 6 What causes the electrons and holes inside a solar cell to move in opposite directions?

6 Hva er årsaken til at elektroner og hull inni en solcelle beveger seg i motsatt retning?

The transfer of charges when a p-type material contacts an n-type material leads to the formation of an internal electric field. Since electrons and holes have opposite effective charges, they move in opposite directions in the field.

## II PROBLEMS - OPPGAVER

All questions should be answered.

NO CREDIT will be given for a correct numerical answer unless the work is shown!!

Alle oppgaver skal besvares.

INGEN POENG gis for riktig tallverdi hvis ikke utledning er vist!!

1. 6 Calculate the power in megawatts during outflow from a tidal power plant that encloses a rectangular area of 1.2x2.5 km, and which fills to a height of 3.7 m above the outlet. Assume an efficiency of 95%, and an emptying time of 2 hours.  
6 Beregn effekten i megawatt under utstrømming i et tidevannskraftverk som dekker et rektangulært område på 1,2x2,5 km, og som fylles til en høyde av 3,7 m over utslippet. Anta 95% effektivitet og at tømning skjer over 2 timer.

$$P = \eta m g h (h/2) / t = (0.95)(1.2 \times 10^3 \text{ m})(2.4 \times 10^3 \text{ m})(3.7 \text{ m})(1.02 \times 10^3 \text{ kg/m}^3)(9.8 \text{ m/s}^2)(3.7 \text{ m}/2) / (3600 \text{ s} \times 2) = 26 \text{ MW}$$

2. 8 The production of a certain resource is increasing at 5% per year, and is predicted to be exhausted in 30 years if this continues (sudden exhaustion, no Hubbert model). A new discovery increases the total known resource by a factor of 5. How many years will it now take to exhaust the resource, assuming the growth rate remains constant?

8) Produksjonen av en gitt ressurs øker med 5% hvert år og spås tom om 30 år hvis trenden fortsetter (plutselig tømming, ingen Hubbellmodell). En ny oppdagelse øker total kjent mengde av ressurser med 5 ganger. Hvor mange år vil det nå ta før det går tomt for ressursen, hvis man antar at vekstraten forblir konstant.

$$N = N_0(1.05)^t \Rightarrow k = \ln(1.05) = 0.048$$

$$Q_T = \int_0^T N_0 e^{kt} dt = \frac{N_0}{k} (e^{kT} - 1)$$

$$5Q_T = \frac{5N_0}{k} (e^{k30} - 1)$$

$$5Q_T = \frac{N_0}{k} (e^{kt_2} - 1)$$

$$5(e^{k30} - 1) = (e^{kt_2} - 1) \quad ;$$

$$e^{kt_2} = (5 * 4.32) - 4 = 17.6$$

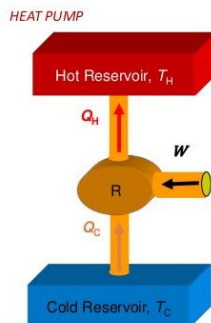
$$t_2 = 59.7 \text{ yrs}$$

3. 2A) Draw a diagram showing energy flow for a heat pump.

2A) Tegn et diagram som viser energiflyten for en varmepumpe.

6B) A particular heat pump uses 1 kW of electrical power. Every second, it removes  $2.5 \times 10^3$  joules from a low temperature reservoir. What is the COP?

6B) En gitt varmepumpe har en effekt på 1 kW. Hvert sekund fjerner den  $2,5 \times 10^3$  joule fra et lav-temperaturreseptat. Hva er COP for varmepumpen?



$$C.O.P. = \frac{Q_H}{Q_H - Q_C} = \frac{3.5 \text{ kW}}{3.5 \text{ kW} - 2.5 \text{ kW}} = 3.5$$

<http://www.slideshare.net/smilingsh ekhar/thermal-engineering-om>

4. 10) How much would the temperature of the earth change (and in what direction) if the albedo were increased by 1%? Assume there is no atmosphere.

10) Hvor mye ville temperaturen til Jorden endre (og i hvilken retning) hvis albedoen ble økt med 1%? Anta ingen atmosfære.

Energy absorbed by earth/area/second has to be same as radiated

$$\frac{1}{4}I_0(1-\alpha) = \varepsilon\sigma T^4$$

$$\frac{1}{4}I_0(1-\alpha_2) = \varepsilon\sigma T_2^4 \quad \text{divide}$$

$$\frac{(1-\alpha)}{(1-\alpha_2)} = \frac{T^4}{T_2^4} = \frac{.69}{.68}$$

$$T/T_2 = 1.0037$$

**Temperature decreases by ~0.4 % .**

(T without atm would be 254; so temperature change ~ 1K)

8The oceans contain about  $1.3 \times 10^{24} \text{ cm}^3$  of water. Deuterium constitutes 0.028% by mass of natural hydrogen. 8Verdenshavene inneholder ca.  $1,3 \times 10^{24} \text{ cm}^3$  vann. For naturlig hydrogen er ca. 0,028% av masen deuterium.

5.

a) What is the total energy in Joules available from this Deuterium by D-D fusion? Assume 4.0 MeV per fusion event.

a)Hva er total mengde tilgjengelig energi ( i joule) fra deuteriumet ved D-D fusjon? Anta 4,0 MeV per fusjonsbegivenhet.

a)( $1.3 \times 10^{24} \text{ cm}^3$ )( $1.02 \text{ g/cm}^3$ )= $1.33 \times 10^{24} \text{ g H}_2\text{O}$ ; ~2/18 of this is hydrogen, and  $2.8 \times 10^{-4}$  of that is Deuterium, so  $4.13 \times 10^{19} \text{ g D}$ . Atomic number 2 -> each 2 grams contains  $6.02 \times 10^{23}$  atoms. It takes two D for each fusion event.

Energy available

$$(1.24 \times 10^{43} \text{ atoms}/2(\text{atoms/fusion}))(4 \times 10^6 \text{ eV/fusion})(1.6 \times 10^{-19} \text{ J/eV}) = \mathbf{3.97 \times 10^{30} \text{ J}}$$

(answers that had correct formulation without numerical values for constants

received full credit)

b) For how many years could fusion reactors with 50% efficiency supply 2.0 million MW?

b)Hvor mange år kan fusjonsreaktorer med 50% effektivitet forsyne 2,0 millioner MW?

b) Reactor energy input per year =  $(1/0.5) (2 \times 10^{12} \text{ J/s}) (3.15 \times 10^7 \text{ s/year}) = 1.26 \times 10^{20} \text{ J}$   
(Total available)/(use per year) ~  $\mathbf{3 \times 10^{10} \text{ years}}$ . The hard parts are extracting the D from the ocean and building the reactors...

6.5The world primary energy usage in 2013 was approximately 13 000 Mtoe.

Assuming that flat panel, non-tracking solar cells at a sunny location can harvest  $8 \text{ kWh/m}^2/\text{day}$ , what area is required (at that location) to supply the energy needs of the earth?

5Verdens primære energibruk i 2013 var ca. 13000 Mtoe. Anta at flate, ikke sporende solceller i et solrikt område kan produsere  $8 \text{ kWh/m}^2/\text{dag}$ . Hvor stort areal (i det solrike området) trengs for å forsyne verdens energibehov?

$$13000 \text{ Mtoe} = 13 \times 10^9 \text{ toe} / (8.6 \times 10^{-5} \text{ toe/kWhr}) = 1.5 \times 10^{14} \text{ kWhr/year}$$

$$(8 \text{ kWhr/day-m}^2) * 365 = 2920 \text{ kWhr/m}^2$$

$$1.5 \times 10^{14} \text{ kWhr} / (2920 \text{ kWhr/m}^2) = \mathbf{5.2 \times 10^{10} \text{ m}^2}$$

## Appendix/Vedlegg

### Energy conversion factors

	J	kWh	Btu	toe
1 Joule (J)	1	$2.78 \times 10^{-7}$	$9.5 \times 10^{-4}$	$2.38 \times 10^{-11}$
1 kilowatt-hr (kWh)	$3.6 \times 10^6$	1	3413	$8.6 \times 10^{-5}$
1 calorie (cal)	4.184	$1.16 \times 10^{-6}$	$3.97 \times 10^{-3}$	$1 \times 10^{-10}$
1 British thermal unit (Btu)	1055	$2.93 \times 10^{-4}$	1	$2.5 \times 10^{-8}$
1 Electron volt (eV)	$1.6 \times 10^{-19}$	$4.45 \times 10^{-26}$	$1.52 \times 10^{-22}$	$3.8 \times 10^{-30}$

### Equations

$$P(t) = \frac{1}{\beta} \left( 1 - \frac{Q(t)}{Q_\infty} \right) Q(t)$$

$$Q(t) = \frac{Q_\infty}{1 + Ae^{-t/\beta}}$$

$$P(t) = P_0 \left( \frac{Q_\infty}{Q_0} \right)^2 \frac{e^{-t/\beta}}{(1 + Ae^{-t/\beta})^2}$$

$$\beta = (Q_\infty - Q_0) \frac{Q_0}{Q_\infty P_0}$$

$$t_m = \left( 1 - \frac{Q_0}{Q_\infty} \right) \frac{Q_0}{P_0} \ln \left( \frac{Q_\infty}{Q_0} - 1 \right)$$

$$P_m = P(t_m) = \frac{Q_\infty^2 * P_0}{4Q_0(Q_\infty - Q_0)}$$

$$Q_T = \frac{N_0}{k} (e^{kT} - 1)$$

$$P = \frac{\Delta E}{\Delta t}$$

$$\eta = 1 - \frac{Q_L}{Q_H}$$

$$\eta_{carnot} = 1 - \frac{T_L}{T_H}$$

$$COP = \frac{Q_H}{Q_H - Q_L} = \frac{T_H}{T_H - T_L}$$

$$E = \frac{hc}{\lambda}; \quad hc = 1.98 \times 10^{-25} \text{ J}\cdot\text{m}$$

$$hc = 1.23 \times 10^{-6} \text{ eV} \cdot \text{m}$$

$$P = I^2 R$$

$$\frac{P}{A} = \varepsilon \sigma T^4 \quad \sigma = 5.67 \times 10^{-8} \text{ Wm}^{-2}\text{K}^{-4}$$

$$I_0 \frac{\pi R^2}{4\pi R^2} = 342 \text{ W / m}^2$$

$$\frac{1}{4} I_0 = \frac{1}{4} \alpha I_0 + I_A$$

$$\lambda_m [\mu\text{m}] = \frac{2898}{T(\text{K})}$$

$$E_{pot} = mgh = \rho Vgh$$

$$E_{kin} = \frac{1}{2} mv^2$$

$$\frac{P}{A} = 6.1 \times 10^{-4} v^3 [\text{kW / m}^2]$$

$$A = \pi r^2 = \pi \left( \frac{d}{2} \right)^2$$

$$\frac{\Delta Q}{\Delta t} = \frac{A}{R} \Delta T = AU\Delta T$$

$$R = 1/k$$

$$Q = mC\Delta T$$

$$m = \rho V$$

$$F = ma = m \frac{\Delta v}{\Delta t}$$

$$V = IR$$

$$P = 0.59 A/2(\rho u^3)$$

$$J = E * cg \sim 1 \text{ kW/m}^3 \text{ s} * T H^2$$

<b>Storage material</b>	<b>MJ per kilogram</b>	<b>MJ per liter (litre)</b>
Uranium-235	83 140 000[3]	1 546 000 000
Hydrogen (compressed at 70 MPa)	123	5.6
Gasoline (petrol) / Diesel	~46	~36
Propane (including LPG)	46.4	26
Fat (animal/vegetable)	37	
Coal	24	
Carbohydrates (including sugars)	17	
Protein	16.8	
Wood	16.2	

Density of water  $1.02 \times 10^3 \text{kg/m}^3$

density of air  $\sim 1.2 \text{kg/m}^3$

acceleration due to gravity  $9.8 \text{m/sec}^2$

Avogadro's number  $6.02 \times 10^{23}$  (# per mole)