

Contact during the exam:
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Exam in FY3403 PARTICLE PHYSICS

Friday December 2, 2011

09:00–13:00

Allowed help: Alternativ C

Standard calculator

K. Rottman: *Matematisk formelsamling* (all languages).

Schaum's Outline Series: *Mathematical Handbook of Formulas and Tables*.

Det finnes også en norsk utgave av dette oppgavesettet.

This problem set consists of 3 pages.

Problem 1. Quark model for baryons

Give a qualitative description of how one in the quark model assumes that baryons are made of quarks. In particular try to explain

- how many quarks and antiquarks the baryons are made of,
- which spin S the total baryon system may have,
- which isospin I the total baryon system may have,
- why there are no baryons with charge -2 (in units of the positron charge),

Problem 2.

The normalized spin/flavor wave function for Δ^{++} with spin $S_z = \frac{3}{2}$ is given by

$$|\Delta^{++} \frac{3}{2}\rangle = |u \uparrow\rangle |u \uparrow\rangle |u \uparrow\rangle.$$

- Find the normalized spin/flavor wave function for Δ^+ with spin $S_z = \frac{3}{2}$.
- Find the normalized spin/flavor wave function for Δ^+ with spin $S_z = \frac{1}{2}$.
- The magnetic moment of a baryon with spin/flavor wave function $|\Psi\rangle$ is defined as

$$\mu_z = \langle \Psi | \sum_i \frac{e Q_i}{2m_i} S_{iz} | \Psi \rangle,$$

where the sum is over the three positions in the wave function. (Note that Q_i , m_i and S_{iz} is operators which take different values depending on the states they act on.)

Find the magnetic moment of Δ^{++} with spin $S_z = \frac{3}{2}$. Assume that $m_u = m_d$.

- Find the magnetic moment of Δ^+ with spin $S_z = \frac{1}{2}$. Assume that $m_u = m_d$.

Hint to point a–b): Use the ladder operators.

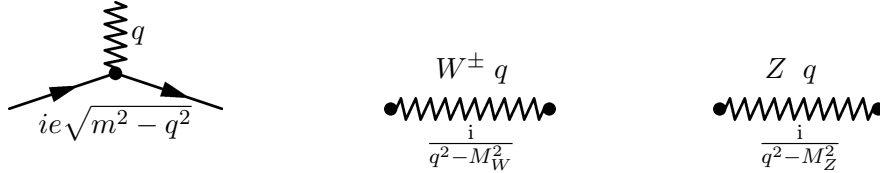
Problem 3. Interaction processes and Feynman diagrams

Draw lowest order Feynman diagrams for the following interaction processes (if the process is possible)

- a) $e^- + \mu^- \longrightarrow e^- + \mu^-$
- b) $e^- + \mu^+ \longrightarrow e^- + \mu^+$
- c) $e^- + \mu^+ \longrightarrow e^+ + \mu^-$
- d) $e^- + e^+ \longrightarrow \mu^+ + \mu^-$
- e) $e^- + e^+ \longrightarrow e^+ + e^-$
- f) $e^- + \nu_\mu \longrightarrow e^- + \nu_\mu$
- g) $e^- + \nu_\mu \longrightarrow \nu_e + \mu^-$
- h) $\tau^- \longrightarrow \mu^- + x$ (replace x by some possible set of particles)
- i) $\nu_e + \nu_\mu \longrightarrow \nu_\mu + \nu_e$
- j) $n \longrightarrow p + x$ (replace x by some possible set of particles)

Problem 4. Elastic $\nu_e + e^- \rightarrow \nu_e + e^-$ scattering

Assume Feynman rules as *indicated* below, where m is the mass of the heaviest fermion involved in the interaction vertex and q is the four-momentum of the virtual messenger particle.



- a) Draw all lowest order Feynman diagrams for the process.
- b) Write down the corresponding algebraic expressions for the scattering amplitude \mathcal{M}_{fi} .
- c) Find the total scattering cross-section. You may assume that $|q^2| \ll M_W^2$ and $|q^2| \ll M_Z^2$ to simplify expressions.

Given:

We use *natural units*, i.e. units where $\hbar = c = 1$. The connection between scattering amplitude \mathcal{M}_{fi} and scattering cross-section is

$$\frac{d\sigma}{d\Omega} = \frac{S}{64\pi^2} \frac{|\mathcal{M}_{fi}|^2}{(E_1 + E_2)^2} \frac{|\mathbf{p}_f|}{|\mathbf{p}_i|}. \tag{1}$$

35. CLEBSCH-GORDAN COEFFICIENTS, SPHERICAL HARMONICS, AND d FUNCTIONS

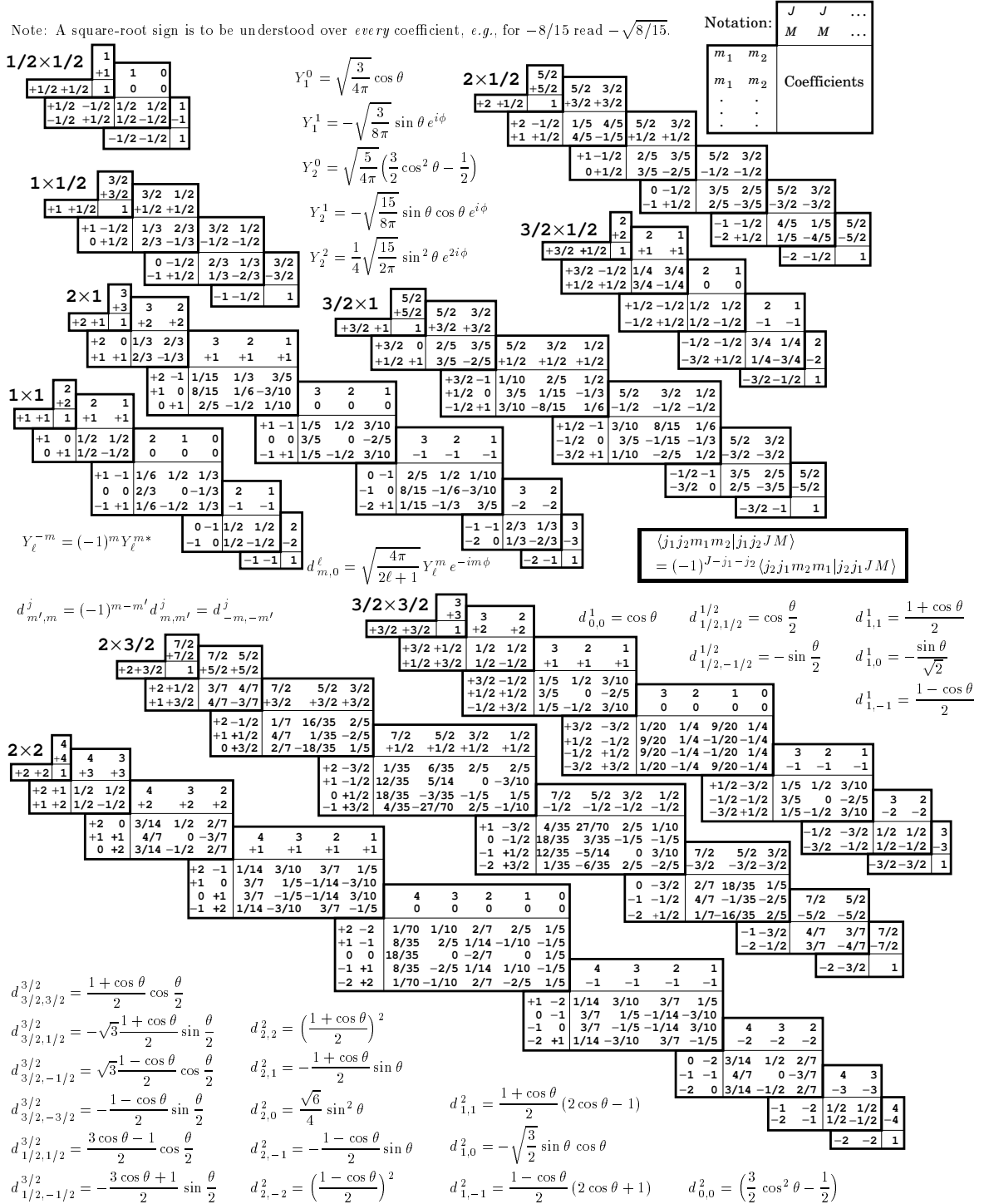


Figure 35.1: The sign convention is that of Wigner (*Group Theory*, Academic Press, New York, 1959), also used by Condon and Shortley (*The Theory of Atomic Spectra*, Cambridge Univ. Press, New York, 1953), Rose (*Elementary Theory of Angular Momentum*, Wiley, New York, 1957), and Cohen (*Tables of the Clebsch-Gordan Coefficients*, North American Rockwell Science Center, Thousand Oaks, Calif., 1974). The coefficients here have been calculated using computer programs written independently by Cohen and at LBNL.