

$$1) \frac{\alpha_p \cancel{f l_T}}{\alpha_v} = \frac{1}{P} \Rightarrow \frac{R T}{P^2 V} = \frac{1}{P} \Rightarrow P = \underline{\underline{\frac{R T}{V}}}$$

2) $\underline{\underline{C}}$. 3) $\underline{\underline{B}}$

$$4) \alpha_L = \frac{1}{L} \left(\frac{\partial L}{\partial T} \right)_P \Rightarrow \alpha_L = \frac{\Delta L / L}{\Delta T} \quad \text{original length}$$

$$\Rightarrow \Delta L = L \cdot \alpha_L \Delta T$$

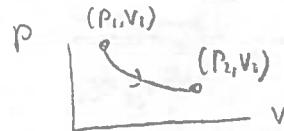
$$\Rightarrow t_2 = 2\pi \sqrt{\frac{L + L \alpha_L \Delta T}{g}} = 2\pi \sqrt{\frac{L (1 + \alpha_L \Delta T)}{g}} = t_1 \sqrt{1 + \alpha_L \Delta T}$$

$$= 15 \sqrt{1 + 20 \cdot 10^{-6} \cdot 10} \approx \underline{\underline{1.0001 \text{ s}}}$$

5) B,C,E 6) B,C 7) A

$$8) L_s = P \cdot t = 500 \frac{J}{s} \cdot 15 \text{ s} = 500 \cdot 15 \text{ J} = 7500 \text{ J} = \underline{\underline{7.5 \text{ kJ}}}$$

9) Adiabat $PV^\gamma = \text{const}$



$$W = \int_{V_1}^{V_2} P dV = \int_{V_1}^{V_2} \frac{\text{const}}{V^\gamma} dV = \text{const} \left[-\frac{V^{1-\gamma}}{1-\gamma} \right]_{V_1}^{V_2} = \frac{\text{const}}{1-\gamma} \left[\frac{V_1}{V_2^\gamma} - \frac{V_2}{V_1^\gamma} \right]$$

$$= \underline{\underline{\frac{1}{1-\gamma} [P_2 V_2 - P_1 V_1]}}$$

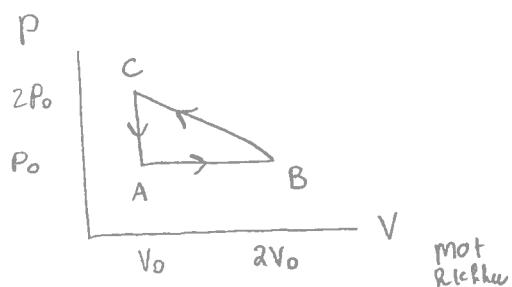
$$10) \text{ H}_2 : \text{Diatomic} \quad f = f_{\text{tors}} + f_{\text{rot}} + f_{\text{vib}} = 3 + 2 + 2$$

Ved 40 K bidrar han translaision $\Rightarrow \underline{\underline{f = 3}}$

$$\Rightarrow C_V = \underline{\underline{\frac{3}{2} R}}$$

$$11) \underline{\underline{E_R = \frac{T_1}{T_2 - T_1}}} \quad 12) \text{ Carnotmaschin} \Rightarrow \eta = 1 - \frac{T_1}{T_2} = \underline{\underline{\frac{T_2 - T_1}{T_2}}}$$

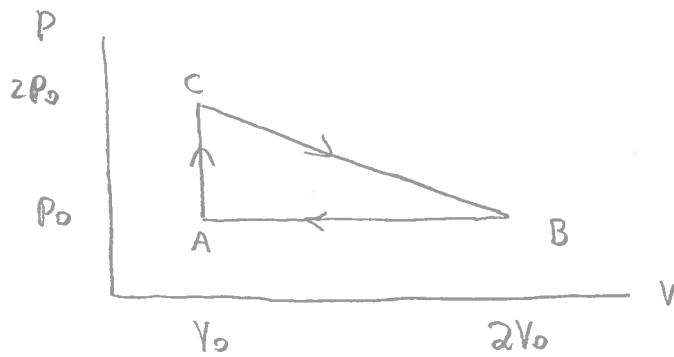
13)



$$Q_t = \Delta U_t + W_t = W_t = -V_0 P_0 \frac{1}{2} = -\frac{1}{2} P_0 V_0$$

$\hookrightarrow > 0$ per sykling

14)



$$\text{Carnots faktor: } n < n_c = 1 - \frac{T_{\text{lavest}}}{T_{\text{høyest}}}$$

Vi må bestemme laveste og høyeste temperatur. $P = \frac{nRT}{V}$

$$\text{Laveste temperatur: } T_A \Rightarrow nRT_A = P_0 V_0$$

Høyeste temp: et eller annet sted på linja fra C til B.

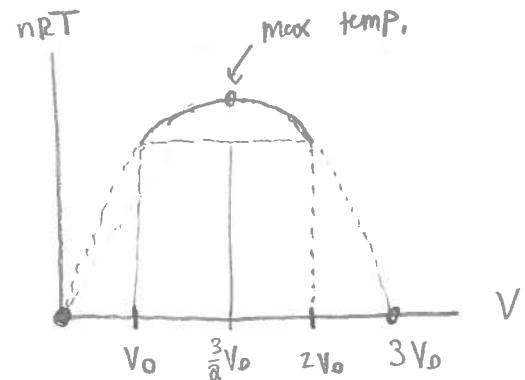
$$\text{Parametrisering: } P_{CB} = -\frac{P_0}{V_0} V_{BC} + 3P_0 \quad (\text{rett linje gir 2 punkt})$$

Temperatur på linja CB:

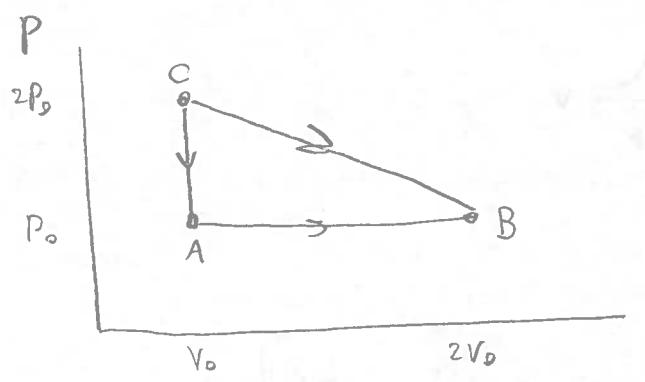
$$nRT = PV = -\frac{P_0}{V_0} V^2 + 3P_0 V = V \left(3P_0 - \frac{P_0}{V_0} V \right) \Rightarrow V = 3V_0$$

$$nRT_{\max} = \frac{3}{2} V_0 \left(3P_0 - \frac{3}{2} P_0 \right) = \frac{3}{2} V_0 \left(\frac{3}{2} P_0 \right) = \frac{9}{4} P_0 V_0$$

$$n_c = 1 - \frac{P_0 V_0}{\frac{9}{4} P_0 V_0} = 1 - \frac{4}{9} = \frac{5}{9} \approx 0.56$$



15)



$$PV = nRT$$

$$dS = \underbrace{C_v dT}_{\frac{nR}{V}} + \underbrace{\left(\frac{\partial P}{\partial T}\right)_V dV}_{nR}$$

$$\frac{P}{nR} = \frac{T}{V}$$

$$\Rightarrow \Delta S = C_v \ln \frac{T_{\text{start}}}{T_{\text{final}}} + nR \ln \frac{V_{\text{final}}}{V_{\text{start}}}$$

$$CA: \text{Isobar}, \Delta T < 0 \Rightarrow \underline{\underline{\Delta S(C \rightarrow A) < 0}}$$

$$AB: \text{Isobar}: \Delta S = C_v \ln \frac{T_B}{T_A} + nR \ln 2 ; \frac{T_A}{V_0} = \frac{T_B}{2V_0} \Rightarrow \frac{T_B}{T_A} = 2$$

$$= \underline{\underline{(C_v + nR) \ln 2}} = C_p \ln 2$$

CB: Samme temperatur i C & B (symmetri, evt ved utregning som i forrige oppgave)

$$\underline{\underline{\Delta S = nR \ln 2}}$$

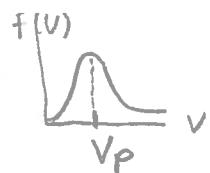
$$\underline{\underline{(C_v + nR) \ln 2}} > \underline{\underline{nR \ln 2}} > \underline{\underline{\Delta S(C \rightarrow A)}}$$

$$\underline{\underline{\Delta S(A \rightarrow B)}} \quad \underline{\underline{\Delta S(C \rightarrow B)}}$$

$$\Rightarrow \underline{\underline{\Delta S(A \rightarrow B) > \Delta S(C \rightarrow B) > \Delta S(C \rightarrow A)}}$$

16) \subseteq

17) Maxwells fartsfordeling



$$f(v) = 4\pi \left(\frac{m}{2\pi kT}\right)^{3/2} v^2 e^{-\frac{mv^2}{2kT}}$$

$$\frac{df}{dv} = \cancel{0} = 4\pi \left(\frac{m}{2\pi kT}\right)^{3/2} \left\{ 2ve^{-\frac{mv^2}{2kT}} + v^2 \cdot e^{-\frac{mv^2}{2kT}} \cdot -\frac{mv}{kT} \right\}$$

$$= 4\pi \left(\frac{m}{2\pi kT}\right)^{3/2} e^{-\frac{mv^2}{2kT}} \underbrace{\left\{ 2 - \frac{mv^2}{kT} \right\}}_0 v$$

$$\Rightarrow \underline{v_p = \sqrt{\frac{2kT}{m}}}$$

$$18) \quad E_2 = \frac{\beta\Delta}{2}$$

to partikler ① ②

$$E_1 = -\frac{\beta\Delta}{2}$$

Mulige tilstander:

① ②

 ,

①

 ,

②

 ,

$$E = \beta\Delta$$

$$E = 0$$

$$E = -\beta\Delta$$

$$E = 0$$

$$\Delta S = S(E=\beta\Delta) - S(E=0) = \underbrace{h \ln 1}_0 - h \ln 2 = -h \underline{\ln 2}$$

$$19) \quad \begin{array}{cccc} \uparrow \downarrow \uparrow & \uparrow \uparrow \downarrow & \uparrow \downarrow \downarrow & \uparrow \downarrow \downarrow \\ \underbrace{\hspace{1cm}}_{E = J/2} & \underbrace{\hspace{1cm}}_0 & \underbrace{\hspace{1cm}}_{-J/2} & \underbrace{\hspace{1cm}}_0 \end{array}$$

$$\begin{array}{cccc} \downarrow \uparrow \uparrow & \downarrow \uparrow \downarrow & \downarrow \downarrow \uparrow & \downarrow \downarrow \downarrow \\ \underbrace{\hspace{1cm}}_0 & \underbrace{\hspace{1cm}}_{-J/2} & \underbrace{\hspace{1cm}}_0 & \underbrace{\hspace{1cm}}_{J/2} \end{array}$$

$$\begin{aligned} Z &= \sum_j e^{-\beta E_j} = 2 e^{-\beta \frac{J}{2}} + 2 e^{\beta \frac{J}{2}} + 4 e^0 \\ &= \underline{\underline{4(1 + \cosh(\beta \frac{J}{2}))}} \end{aligned}$$

$$20) \quad F = F_i + h_T B_2(T) \frac{N^2}{V}$$

$$P = - \left(\frac{\partial F}{\partial V} \right)_T \quad \text{Frw TDI}$$

$$\left(\frac{\partial F}{\partial V} \right)_T = \left(\frac{\partial F_i}{\partial V} \right)_T - h_T B_2(T) \frac{N^2}{V^2}$$

$$P = \underline{\underline{N \frac{h_T}{V} + N \frac{h_T}{V} \cdot \frac{N}{V} B_2(T) = \frac{N h_T}{V} \left(1 + \frac{N}{V} B_2(T) \right)}}$$

$$21) \quad S = - \left(\frac{\partial F}{\partial T} \right)_V$$

$$\left(\frac{\partial F}{\partial T} \right)_V = \left(\frac{\partial F_i}{\partial T} \right)_V + h \frac{N^2}{V} \left\{ B_2(T) + T \frac{dB_2}{dT} \right\}$$

$$\Rightarrow S = S_i - \underline{\underline{\frac{h N^2}{V} \left\{ B_2(T) + T \frac{dB_2}{dT} \right\}}}$$

$$22) B_2(T) = -\frac{a}{kT}$$

$$\frac{dB_2}{dT} = \frac{a}{kT^2} ; \quad \frac{d^2B_2}{dT^2} = -\frac{2a}{kT^3}$$

$$C_v = C_{v,i} - h \frac{N^2}{V} T \left(\frac{2a}{kT^2} + -\frac{2a}{kT^2} \right) = C_{v,i} = \frac{3}{2} h$$

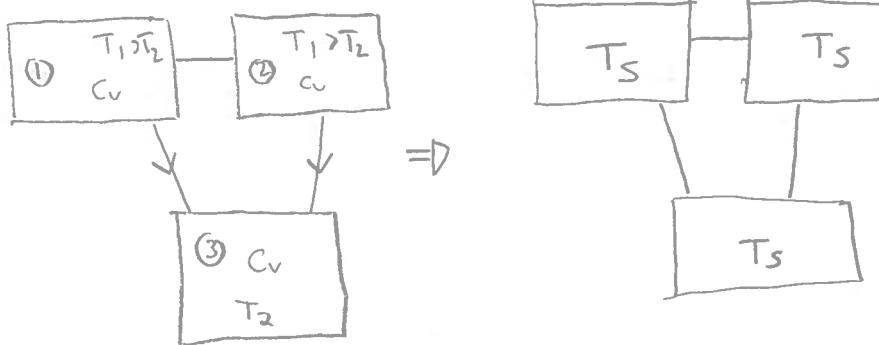
EPP: Kun bidrag fra translasjon ved alle temperaturer
 \Rightarrow gassen må være monatomisk

23) A, B, C, D, E Alt er ekvivalent

$$24) dS = C_v \frac{dT}{T} + \underbrace{\frac{nR}{V} dV}_0 \Rightarrow \Delta S = C_v \ln \frac{T_{\text{sup}}}{T_{\text{mvt}}}$$

$$\Rightarrow \Delta S = C_v \ln \frac{T_{\text{O12}}}{T_0} = C_v \ln \frac{1}{2} = -C_v \ln 2 = -\underline{\underline{\frac{3}{2} N h \ln 2}}$$

25)



$$Q = \Delta U + W \Rightarrow \Delta U = \Delta U_{①} + \Delta U_{②} + \Delta U_{③} = 0$$

$$\Rightarrow T_s = \frac{T_1 + T_2 + T_1}{3} = \frac{2T_1 + T_2}{3}$$

$$\Delta S = \Delta S_{①} + \Delta S_{②} + \Delta S_{③} = 2C_v \ln \frac{T_s}{T_1} + C_v \ln \frac{T_s}{T_2} = C_v \ln \frac{T_s^3}{T_1^2 T_2}$$

$$= C_v \ln \frac{(2T_1 + T_2)^3}{9T_1^2 T_2}$$

$$26) \quad dW = -f dL$$

$$P \rightarrow -f, V \rightarrow L$$

$$S(L, T) = g(T) - c \left(\frac{L^2}{2L_0} + \frac{L_0^2}{L} \right)$$

$$dF = -S dT + -P dV$$

$$\Rightarrow \left(\frac{\partial S}{\partial V} \right)_T = \left(\frac{\partial P}{\partial T} \right)_V$$

$$\Rightarrow \left(\frac{\partial S}{\partial L} \right)_T = - \left(\frac{\partial f}{\partial T} \right)_L$$

$$+ \left(\frac{\partial f}{\partial T} \right)_L = + c \left(\frac{L}{L_0} - \frac{L_0^2}{L^2} \right)$$

$$\Rightarrow f(T, L) = CT \left(\frac{L}{L_0} - \frac{L_0^2}{L^2} \right) + h(L)$$

$$f(T, L=L_0) = 0 = CT(1-1) + h(L) \Rightarrow h(L) = 0$$

$$\Rightarrow \underline{f(T, L) = CT \left(\frac{L}{L_0} - \frac{L_0^2}{L^2} \right)}$$

$$27) \quad U = \alpha V T^4$$

$$T dS = dU + PdV = \left(\frac{\partial U}{\partial V}\right)_T dV + \left(\frac{\partial U}{\partial T}\right)_V dT + PdV \\ = (\alpha T^4 + P) dV + 4\alpha V T^3 dT$$

$$\Rightarrow dS = \underbrace{\left(\frac{P}{T} + \alpha T^3\right)}_{S(T)} dV + \underbrace{4\alpha V T^3 dT}_{}$$

$$S = V \cdot S(T)$$

$$dS = \left(\frac{\partial S}{\partial V}\right)_T dV + \left(\frac{\partial S}{\partial T}\right)_V dT = \underbrace{S(T) dV}_{\text{ }} + \underbrace{\left(\frac{\partial S}{\partial T}\right)_V dT}_{\text{ }}$$

$$\Rightarrow S(T) = \alpha T^3 + \underline{P} \quad \text{og} \quad \left(\frac{\partial S}{\partial T}\right)_V = 4\alpha V T^2$$

$$\Rightarrow S(T, V) = \frac{4}{3} \alpha V T^3 + f(V) \\ L > 0 \quad (\text{initial temperature})$$

$$= \underline{\underline{\frac{4}{3} \alpha V T^3}}$$

$$28) \quad P = \frac{\alpha}{3} T^4$$

$$H = U + PV = \alpha V T^4 + \frac{\alpha}{3} V T^4 = \frac{4}{3} \alpha V T^4 = 4PV$$

$$C_P = \left(\frac{\partial H}{\partial T}\right)_P = 4P \left(\frac{\partial V}{\partial T}\right)_P = 4P \left(\frac{\partial T}{\partial V}\right)_P^{-1}$$

$$\left(\frac{\partial T}{\partial V}\right)_P \Rightarrow T(V, P) = \left(\frac{3P}{\alpha}\right)^{1/4} \Rightarrow \left(\frac{\partial T}{\partial V}\right)_P = 0 \Rightarrow \left(\frac{\partial V}{\partial T}\right)_P = \infty$$

$$\Rightarrow \underline{\underline{C_P = \infty}}$$

$$29) \quad dG = Vdp - SdT + \mu dN \quad ; \quad G = \mu N$$

$$= Nd\mu + \mu dN$$

$$PV = NkT \Rightarrow \frac{N}{V} = \frac{P}{kT}$$

$$\Rightarrow Nd\mu = Vdp - SdT$$

$$\int \frac{dy}{dx} dx$$

$$\Rightarrow \frac{N}{V} = \left(\frac{dp}{d\mu} \right)_T = \frac{P}{kT}$$

$$\Rightarrow \left(\frac{\partial \mu}{\partial P} \right)_T = \frac{kT}{P}$$

$$\Rightarrow \mu - \mu_0 = kT \ln \frac{P}{P_0}$$

$$\Rightarrow \mu = \mu_0 + kT \ln \frac{P}{P_0}$$

30) Siden de stoichiometriske tallene alle er 1
er LV-betingelsen ~~af alle kemiske potensial~~
~~skal være like. Dvs. ettersatt~~ $\underline{\underline{C}}$

$$\mu(A) + \mu(B) = \mu(C) + \mu(D)$$

$$\Rightarrow eneste mulighet er \underline{\underline{C}}$$

31) Ideell blanding:

$$\mu_j = \mu_j^\circ + RT \ln x_j$$

Mcbrøgh Salt: x

\Rightarrow Mcbrøgh Vann: $1-x$

$$\text{LV: } \underbrace{\mu_{H_2O}^\circ(P, T)}_{\mu_{H_2O}^\circ(P + \Delta P, T) + \underbrace{RT \ln(1-x)}_{-\bar{R}T x}} \quad (\text{ideell blanding})$$
$$\mu_{H_2O}^\circ(P, T) + \Delta P \left(\frac{\partial \mu_\circ}{\partial P} \right)_T$$

$$\Rightarrow \frac{RT x}{\Delta P} = \underbrace{\left(\frac{\partial \mu_{H_2O}^\circ}{\partial P} \right)_T}_{\frac{V_{H_2O}}{N_{H_2O}}} \approx \frac{V}{N}$$

$$\Rightarrow \frac{RT}{\Delta P} \frac{N_{\text{salt}}}{N} = \frac{V}{N} \Rightarrow \underline{\underline{\Delta P = \frac{N_{\text{salt}} RT}{V}}}$$

32) A, B

C er feil fordi at hvasistatiske prosesser hvor vi ikke ser bort fra dissipative effekter (f.eks friksjon) ikke er tenkbare.

$$33) T ds = C_v dT + T \left(\frac{\partial P}{\partial T} \right)_v dv$$

$P \rightarrow -\mu_0 \cancel{sl}$, $v \rightarrow M$

$$M = C \frac{\cancel{sl}}{T} \Rightarrow \cancel{sl} = \frac{M T}{C}$$

$$\Rightarrow T ds = \underbrace{C_M dT}_{\left(\frac{\partial M}{\partial T} \right)_M = 0} - T \mu_0 \underbrace{\left(\frac{\partial H}{\partial T} \right)_M}_{\frac{M}{C}} dM = -T \frac{\mu_0}{C} M dM$$

$$\Rightarrow \int_{S_0}^S ds = - \frac{\mu_0}{C} \int_0^M M dM = - \frac{\mu_0 M_1^2}{2C}$$

$$\Rightarrow \Delta S = - \frac{\mu_0 M_1^2}{2C}$$

34) B

$$35) dT = \frac{\mu_0 T}{C \cancel{sl}} \left| \left(\frac{\partial M}{\partial T} \right)_{\cancel{sl}} \right| d\cancel{sl}$$

$$C \cancel{sl} = \left(\frac{\partial H}{\partial T} \right)_{\cancel{sl}} = \frac{\partial}{\partial T} \left\{ -\mu_0 \cancel{sl} \cdot C \left(\frac{\cancel{sl}}{T} \right)^\alpha \right\}$$

$$= -\mu_0 C \cancel{sl}^{\alpha+1} \cdot -\alpha \frac{1}{T^{\alpha+1}} = \alpha \mu_0 C \left(\frac{\cancel{sl}}{T} \right)^{\alpha+1}$$

$$\left(\frac{\partial M}{\partial T} \right)_{\cancel{sl}} = \frac{\partial}{\partial T} \left\{ C \frac{\cancel{sl}^\alpha}{T^\alpha} \right\} = C \cancel{sl}^\alpha \frac{\partial}{\partial T} \left\{ T^{-\alpha} \right\} = C \cancel{sl}^\alpha \cdot -\alpha \frac{1}{T^{\alpha+1}}$$

$$dT = \mu_0 T \cdot \frac{T^{\alpha+1}}{\cancel{sl}^{\alpha+1} \alpha \mu_0 C} \cdot \frac{-\alpha e^{\cancel{sl}^\alpha}}{T^{\alpha+1}} d\cancel{sl} \frac{T}{\cancel{sl}} d\cancel{sl}$$

$$\Rightarrow \frac{dT}{T} = \frac{d\cancel{sl}}{\cancel{sl}} \Rightarrow \ln T = \ln \cancel{sl} + C$$

$$\underline{\underline{T = A \cancel{sl}}}$$

36)

$$V = \frac{RT}{P} + \left(b - \frac{a}{RT} \right)$$

$$\mu_{JT} = \frac{1}{C_P} \left[T \left(\frac{\partial V}{\partial T} \right)_P - V \right]$$

$$= \frac{1}{C_P} \left[T \left(\frac{R}{P} + \frac{a}{RT^2} \right) - V \right] = \frac{1}{C_P} \left[\frac{RT}{P} + \frac{a}{RT} - V \right]$$

$$= \frac{1}{C_P} \left[T - b + \frac{a}{RT} + \frac{a}{RT} - V \right] = \frac{1}{C_P} \left[\frac{2a}{RT} - b \right]$$

inversions temperatur: $\mu_{JT}(T_x) = 0$

$$\Rightarrow \frac{2a}{RT_x} - b = 0 \Rightarrow T_x = \underline{\underline{\frac{2a}{Rb}}}$$

$$37) P = \frac{NkT}{V-Nb} - a \frac{N^2}{V^2}$$

$$\frac{\partial P}{\partial V} = - \frac{NkT}{(V-Nb)^2} + 2a \frac{N^2}{V^3} \Rightarrow \frac{NkT_c}{(V-Nb)^2} = 2a \frac{N^2}{V^3} \quad (1)$$

$$\frac{\partial^2 P}{\partial V^2} = 2 \frac{NkT}{(V-Nb)^3} - 6a \frac{N^2}{V^4} \Rightarrow \frac{NkT_c}{(V-Nb)^3} = 3a \frac{N^2}{V^4} \quad (2)$$

$$\Rightarrow \frac{(1)}{(2)} = \frac{\frac{NkT_c}{(V_c-Nb)^2}}{\frac{NkT_c}{(V_c-Nb)^3}} \cdot \frac{(V_c-Nb)^3}{3a \frac{N^2}{V^4}} = (V_c-Nb) = \frac{2aN^2}{V_c^3} \cdot \frac{V_c^4}{3aN^2} = \frac{2}{3} V_c$$

$$\Rightarrow \frac{V_c}{3} = Nb \Rightarrow V_c = 3 \underline{\underline{Nb}}$$

$$\Rightarrow NkT_c = 2a \frac{N^2}{3^3 N^2 b^3} \cdot (2Nb)^2 = \frac{2a}{27Nb^3} \cdot 4N^2 b^2$$

$$= \frac{8aN}{27b} \Rightarrow T_c = \underline{\underline{\frac{8a}{27kb}}}$$

$$38) P = \frac{RT}{V-b} - \frac{a}{V^2}$$

$$dU = \underbrace{\left(\frac{\partial U}{\partial T}\right)}_{C_V} dT + \underbrace{\left(\frac{\partial U}{\partial V}\right)}_{\alpha} dV$$

$$T \left(\frac{\partial P}{\partial T}\right)_V - P = \frac{RT}{V-b} - P = \frac{a}{V^2}$$

$$dU = C_V dT + \alpha \frac{dV}{V^2}$$

$$\Rightarrow U - U_0 = C_V T - \frac{a}{V} \Rightarrow U = C_V T - \frac{a}{V} + U_0$$

$$39) \frac{dP}{dT} = \frac{l}{T \Delta V} = \frac{L_F}{T \Delta V} \quad \Delta V = V_g - V_v \approx V_g = \left(\frac{AT}{P}\right)^2$$

$$\frac{dP}{dT} = \frac{L_F}{A^2 T^3} \frac{P^2}{P_1} \Rightarrow \int_{P_1}^P \frac{dP}{P^2} = \frac{L_F}{A^2} \int_{T_1}^T \frac{dT}{T^3}$$

$$= - \left[\frac{1}{P} - \frac{1}{P_1} \right] = \frac{L_F}{A^2} \left[-\frac{1}{2} T^{-2} \right]_{T_1}^T = -\frac{L_F}{2A^2} \left[\frac{1}{T^2} - \frac{1}{T_1^2} \right]$$

$$\Rightarrow \frac{1}{P} - \frac{1}{P_1} = \frac{L_F}{2A^2} \left(\frac{1}{T^2} - \frac{1}{T_1^2} \right)$$

$$40) P \rightarrow -\mu_0 \delta e \quad V \rightarrow M$$

$$-\mu_0 \frac{d\delta e}{dT} = \frac{\Delta S}{\Delta M} \Rightarrow \Delta S = -\mu_0 \underbrace{\Delta M}_{\text{positiv}} \cdot \frac{d\delta e}{dT}$$

$$A: \Delta S > 0 \quad B: \Delta S = 0 \quad C: \Delta S < 0 \quad D: \Delta S = 0 \quad E: \Delta S = +\infty$$

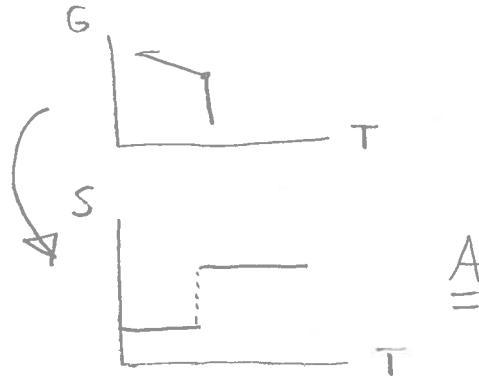
$$\underline{\underline{\Delta S_E > \Delta S_A > \Delta S_B = \Delta S_D > \Delta S_C}}$$

$$41) G = U + PV - TS$$

$$TdS = dU + PdV$$

$$dG = dU + PdV + VdP - TdS - SdT = VdP - SdT$$

$$\Rightarrow S = - \left(\frac{\partial G}{\partial T} \right)$$

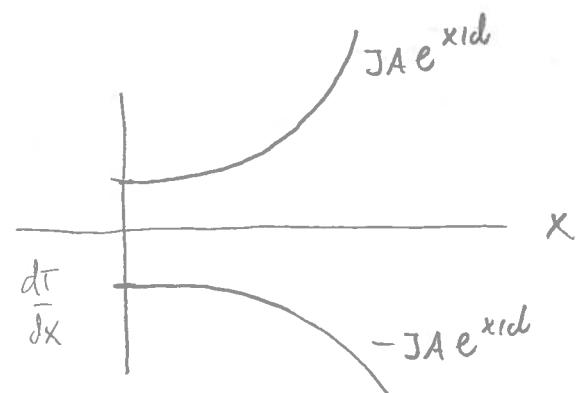


$$42) \Delta T = J \sum_{i=1}^N \frac{a_i}{h_i} = J \left(\frac{b_1}{h_1} + \frac{b_2}{h_2} \right)$$

$$J = \frac{20}{\frac{1}{0.14} + \frac{2}{0.047}} = 0.40 \frac{W}{m^2}$$

$$43) J = -f_l(x) \frac{dT}{dx} \quad \text{siden engi er bekvæmt er } J = \text{konst. i 1D}$$

$$\Rightarrow \frac{dT}{dx} = - \frac{J}{f_l(x)} = -JAe^{x/d}$$



$\frac{dT}{dx}$ blir mindre og mindre med økende x

\Rightarrow Eneste mulighet er B

$$44) \nabla \cdot J = 0 \quad J = -\kappa \nabla T$$

$$0 = \frac{dJ}{dx} = \frac{d}{dx} \left(-\kappa \frac{dT}{dx} \right)$$

$$\Rightarrow 0 = \frac{d\kappa}{dx} \frac{dT}{dx} + \kappa \frac{d^2T}{dx^2}$$

$$\kappa(x) = A e^{-x/d}$$

$$\frac{d\kappa}{dx} = A e^{-x/d} \cdot -\frac{1}{d} = -\frac{A}{d} e^{-x/d}$$

$$\Rightarrow 0 = -\frac{A}{d} e^{-x/d} \frac{dT}{dx} + A e^{-x/d} \frac{d^2T}{dx^2}$$

$$\Rightarrow 0 = \frac{d^2T}{dx^2} - \frac{1}{d} \frac{dT}{dx}$$

$$45) \text{ Symmetrisk fordeling} \Rightarrow \langle \hat{F} \rangle = \langle \hat{F}^2 \rangle = 0$$

$$\langle \vec{r}^2 \rangle = \langle x^2 + y^2 \rangle = \iint_{-\infty}^{\infty} (x^2 + y^2) \tilde{P}(x, y, t) dx dy$$

$$= \iint_{0}^{\infty} r^2 \cdot \frac{1}{4\pi D t} e^{-\frac{r^2}{4Dt}} r dr d\theta$$

$$= \frac{2\pi}{4\pi Dt} \int_0^\infty r^3 e^{-\frac{r^2}{4Dt}} dr$$

$$= \frac{1}{2Dt} \frac{16D^2t^2}{2} = 4Dt$$

$$\Rightarrow \text{Var}(F) = \langle \hat{F}^2 \rangle - \langle \hat{F} \rangle^2 = \underline{\underline{4Dt}}$$