

Problem 1.

Two solutions to the problem are provided in the *code* subdirectory. One in Fortran (listing 1) and one in C (listing 2).

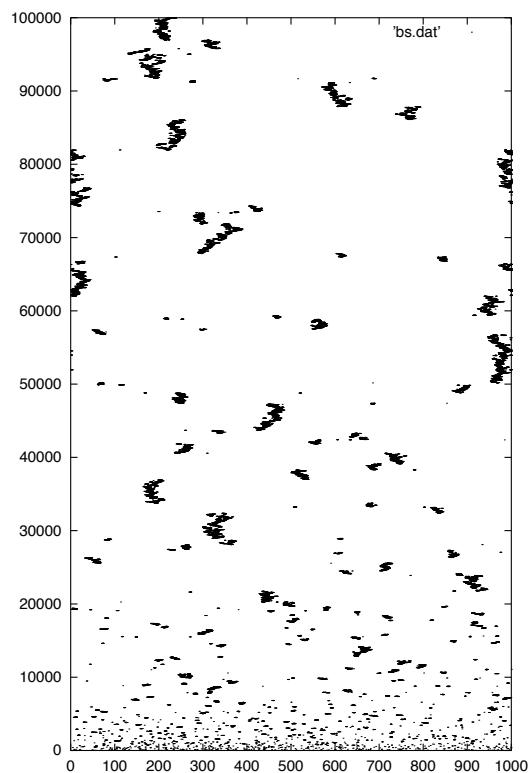


Figure 1: Results from the Bak-Sneppen model.

There are two aspects of this program that is not straight forward: 1) The implementation of the random number generator. This is a so-called portable generator that goes under the name "16807" and which works by overflow. We will describe this in detail later on in the course. The second aspect is the implementation of the periodic boundary conditions. The way I have implemented them is the most efficient: There are no logical tests to perform. In the plot in figure 1 I have reproduced Fig. 3a in the Bak-Sneppen paper. It shows clearly how the activity in the model is "clumped" together. This clumping corresponds to the avalanches of change (think about this!). Here the x-axis shows position and the y-axis shows time.

Listing 1: Implementation of the Bak-Sneppen model in Fortran

```

1      program bs
2 c
3 c Program implementing Bak-Sneppen model
4 c
5      parameter(l=1000,mtime=100000,idum=4711)
6 c
7      dimension fitnes(l),ir(l),il(l)
8 c
9 c Heating up random number generator
10 c
11     ibm=idum
12     rinv=0.5/(2.***31-1.)
13     do i=1,1000
14     ibm=ibm*16807
15     enddo
16 c
17 c Implementing periodic boundary conditions
18 c
19     do i=1,l
20     ir(i)=i+1
21     il(i)=i-1
22     enddo
23     ir(l)=1
24     il(1)=l
25 c
26 c Initializing fitness vector
27 c
28     do i=1,l
29     ibm=ibm*16807
30     fitnes(i)=(ibm*rinv+0.5)
31     enddo
32 c
33 c Loop over time
34 c
35     do itime=1,mtime
36 c
37 c finding smallest fitness factor
38 c
39     is=0
40     fs=2.0
41     do i=1,l
42     if(fitnes(i).le.fs) then
43     is=i
44     fs=fitnes(i)
45     endif
46     enddo
47 c
48 c Updating element with smallest fitness and neighbors
49 c
50     ibm=ibm*16807
51     fitnes(   is )=(ibm*rinv+0.5)

```

```

52     ibm=ibm*16807
53     fitnes(ir(is))=(ibm*rinv+0.5)
54     ibm=ibm*16807
55     fitnes(il(is))=(ibm*rinv+0.5)
56 c
57 c Writing position of least fit element
58 c
59     write(*,*) is,itime
60 c
61     enddo
62 c
63     end

```

Listing 2: Implementation of the Bak-Sneppen model in C

```

1 #include<stdio.h>
2 #include<stdlib.h>
3 #include<sys/time.h>
4 #include<math.h>
5
6 // RNG Variables and constants
7 const double RINV = 0.5/(1 << 31);           // 0.5/(2^31)
8 int IBM;
9
10 // Variables and constants
11 int N;
12 int dtmax;
13
14 int mini;
15 double minr;
16 double t_tmp;
17 double time_init, time_sim, time_out;
18
19 // Arrays
20 double * r;        // Array for storing fitness values
21 int * mins;        // Array for storing which species was least fit
22
23
24 double walltime ( void ) { // Returns current time, with microsecond
25     precision
26     static struct timeval t;
27     gettimeofday ( &t, NULL );
28     return ( t.tv_sec + 1e-6 * t.tv_usec );
29 }
30
31 int randIBM() {      // Random integer between -2^31 and 2^31 - 1
32     IBM*=16807;       // google: LCG - Linear Congruential Generator
33     return IBM;
34 }
35
36 double randIBMf() { // Random number between 0 and 1, [0,1)
37     return randIBM()*RINV + 0.5;
38 }

```

```
38
39 int main (int argc, char ** argv) {
40     int i,j;
41
42     // INITIALIZATIONS
43     t_tmp = walltime();
44     for (i = 0; i < argc; i++) {
45         printf("%s ",argv[i]);
46     }
47     printf("\n");
48
49     if (argc == 1) {
50         printf("No arguments from command line. Using default values\n"
51             );
52         N = 64;
53         dtmax = 10000;
54     } else if (argc == 3) {
55         N = atoi(argv[1]);           // First argument, number of species
56         dtmax = atoi(argv[2]);      // Second argument, number of
57             iterations
58     } else {
59         printf("Invalid number of arguments from command line,
60             aborting.\n");
61         exit(-1);
62     }
63     printf(" N = %d\n",N);
64     printf(" dtmax = %d\n\n",dtmax);
65
66     // Initializing RNG
67     IBM = 2*time(0) + 1;
68     for (i = 0; i < 1000; i++)
69         randIBM();
70
71     r = (double*)malloc(sizeof(double)*N);
72     mins = (int*)malloc(sizeof(int)*dtmax);
73
74     // Initialize fitness array
75     for(i = 0; i < N; i++){
76         r[i] = randIBMf();
77     }
78     time_init = walltime() - t_tmp;
79
80     // MAIN LOOPS
81     t_tmp = walltime();
82     for(j = 0;j < dtmax; j++){
83         minr = 1;
84         for(i=0;i<N;i++){
85             if (r[i] < minr){
86                 minr = r[i];
87                 mini = i;
88             }
89         }
90     }
91 }
```

```
88     }
89
90     mins[j] = mini;
91     int right = mini + 1;
92     int left = mini - 1;
93
94     if(mini == N-1)
95         right = 0;
96     if(mini == 0)
97         left = N-1;
98
99     r[mini] = randIBMf();
100    r[left] = randIBMf();
101    r[right] = randIBMf();
102}
103 time_sim = walltime() - t_tmp;
104
105 // PRINT TO FILE
106 t_tmp = walltime();
107 for (i = 0; i < dtmax; i++){
108     fprintf(f1, "%d      %d\n", mins[i], i);
109 }
110 time_out = walltime() - t_tmp;
111
112 // TIMINGS
113 printf("time init: %f\n", time_init);
114 printf("time sim: %f\n", time_sim);
115 printf("time out: %f\n", time_out);
116
117 // FREE MEMORY
118 free(r);
119 free(mins);
120 fclose(f1);
121 return 0;
122}
```