TFY4240

Problemset 1 Autumn 2014



Problem 1.

Do all the examples of chapter 2 of Griffith. This is intended for helping you to recapitulate what you already should know from previous classes.

Problem 2.

By using the index notation (and the Levi-Civita symbol) introduced in the lectures, show the following vector identities:

a) $\mathbf{A} \times (\mathbf{B} \times \mathbf{C}) = \mathbf{B}(\mathbf{A} \cdot \mathbf{C}) - \mathbf{C}(\mathbf{A} \cdot \mathbf{B})$

b)
$$\boldsymbol{\nabla} \cdot (\boldsymbol{\nabla} \times \mathbf{A}) = 0$$

c)
$$\nabla \times (\nabla \psi) = 0$$

- d) $\nabla \times (\nabla \times \mathbf{A}) = \nabla (\nabla \cdot \mathbf{A}) \nabla^2 \mathbf{A}$
- e) $\nabla \times \left(\frac{A}{g}\right) = \frac{g(\nabla \times \mathbf{A}) + \mathbf{A} \times (\nabla g)}{g^2}$