## TFY4240

Problemset 5 Autumn 2014

## Problem 1.

Consider an infinitesimal static magnetic dipole of magnetic dipole moment $\boldsymbol{m}$. In a coordinate system centered at the dipole, the vector potential associated with can in the Coulomb gauge be written

$$
\begin{equation*}
\boldsymbol{A}(\boldsymbol{r})=\frac{\mu_{0}}{4 \pi} \frac{\boldsymbol{m} \times \hat{\boldsymbol{r}}}{r^{2}} \tag{1}
\end{equation*}
$$

a) Use expression (1) to obtain an expression for the magnetic induction, $\boldsymbol{B}(\boldsymbol{r})$. Express your answer in coordinate free form.
b) Compare your answer from the previous subproblem with the expression for the electric field from a static electric dipole.

## Problem 2.



An infinitely long wire carries a (time-independent) current $I$. The wire is bent so as to have a semi-circular detour, of radius $R$, around the origin $O$ (see figure).
a) Derive an expression for the magnetic field (vector), $\mathbf{H}$, at the origin $O$ of the coordinate system.
b) Determine the numeric value of this magnetic field given the current $I=1 \mathrm{~A}$ and radius $R=1 \mathrm{~cm}$.

## Problem 3.

Examples 6.1 and 6.3 from Griffiths.

