



# Cosmic Ray Acceleration in Relativistic Astrophysical Shocks

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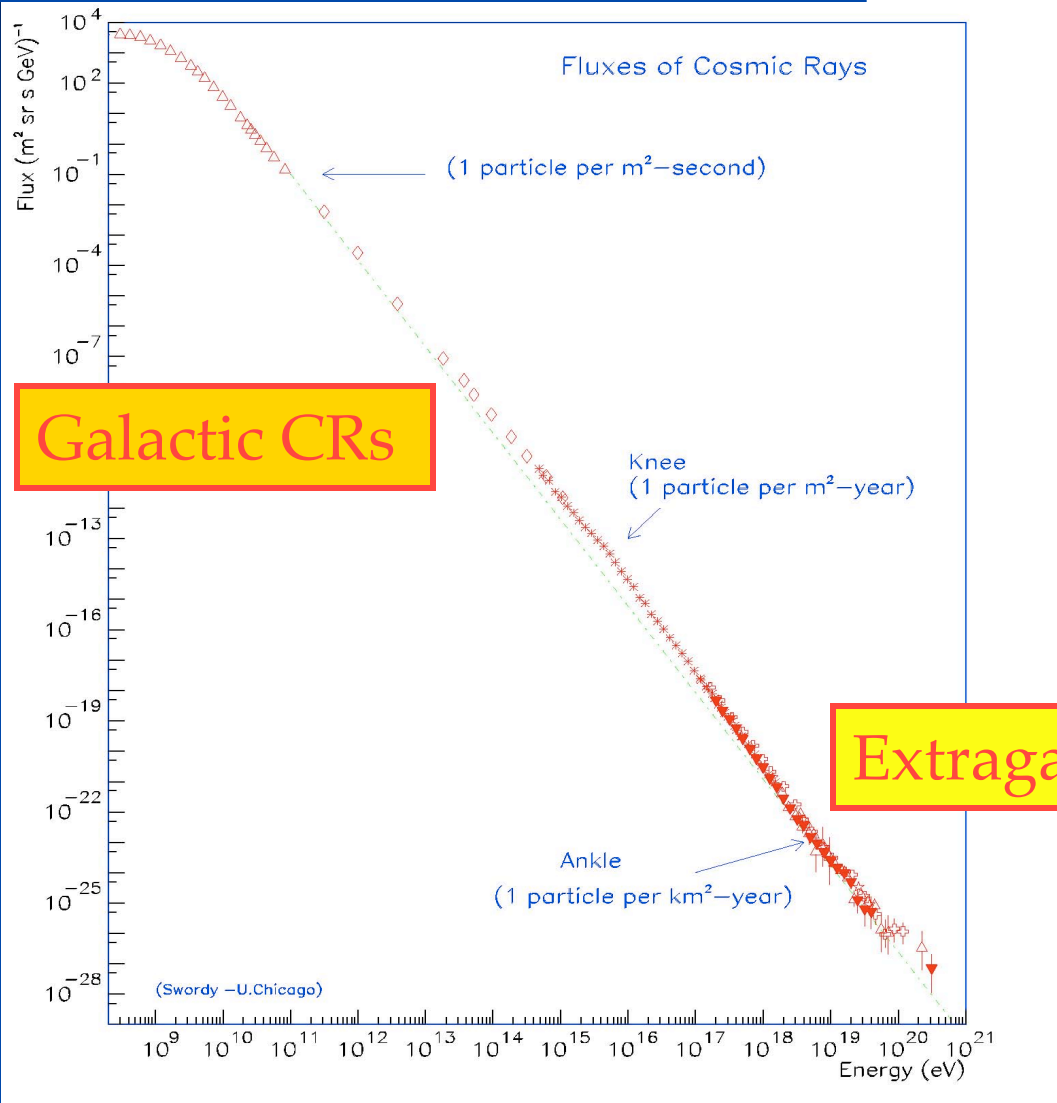
SOCOR Conference, Trondheim, Norway, 16<sup>th</sup> June, 2009

# Talk Layout

- Astrophysical context; gamma-ray bursts, and active galaxies (radio galaxies and blazars) as sources of ultra-high energy cosmic rays (UHECRs);
- Monte Carlo simulation technique;
- Plane-parallel relativistic shocks;
- Oblique shocks;
- Bottom line: a plethora of possibilities (=everyone can have their flavor of coffee).

# Complete Cosmic Ray Spectrum

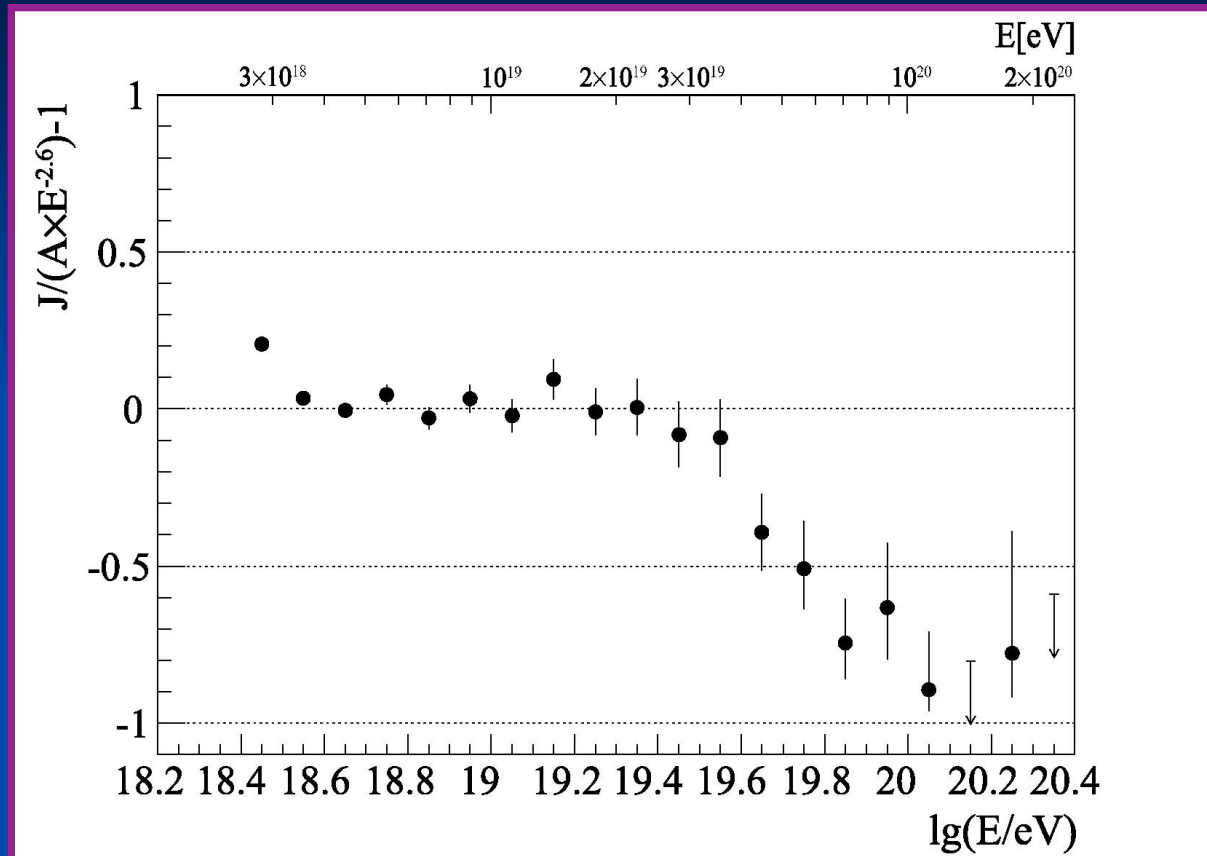
Balloon + satellite expts ← | → EAS arrays



Discovered in 1912 by V. Hess

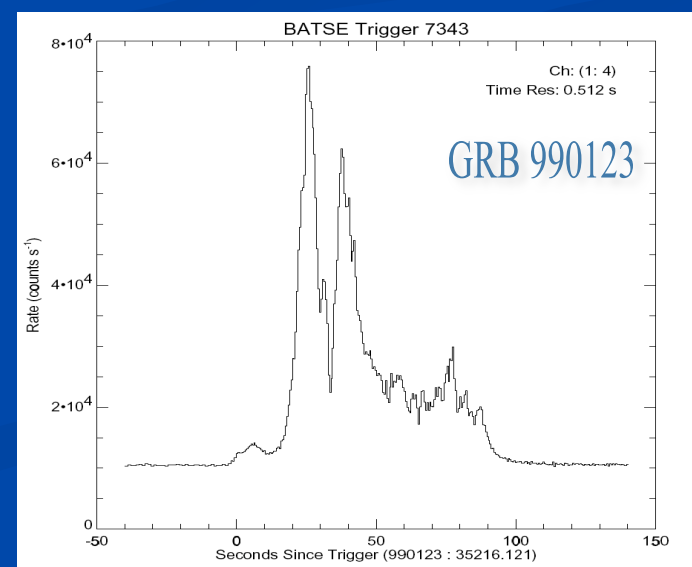
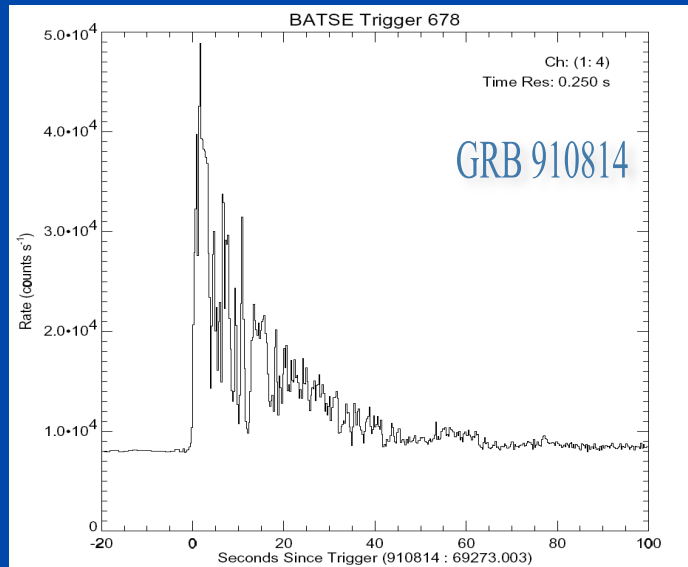
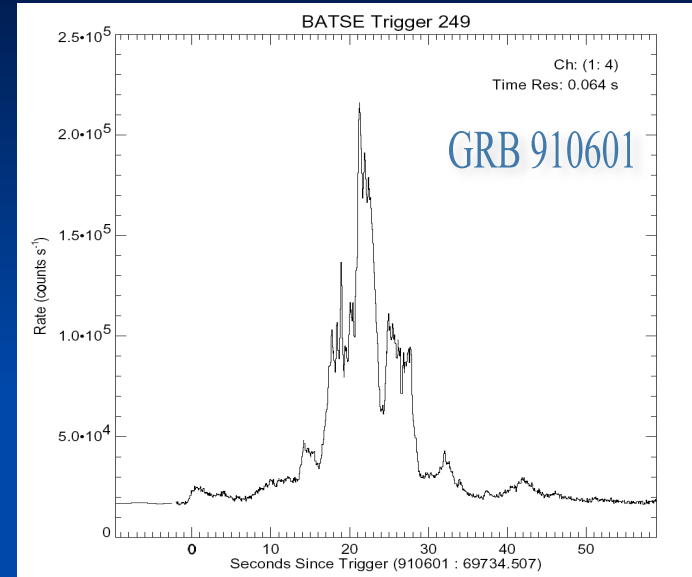
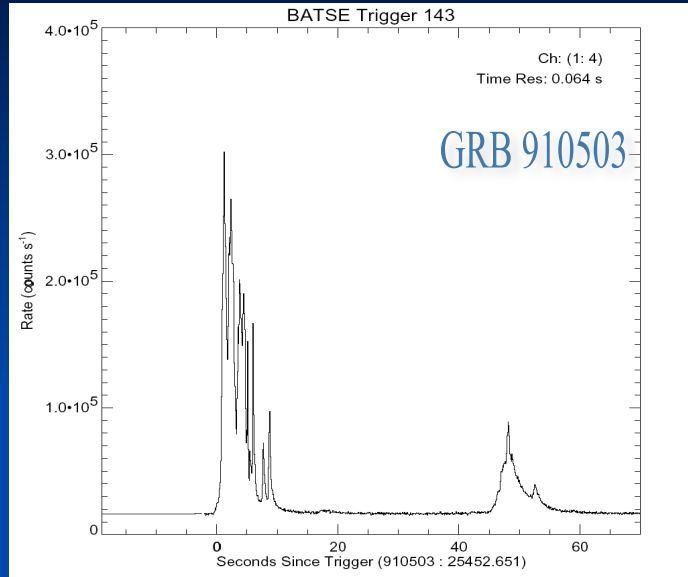
Extragalactic CRs

# Pierre Auger UHECR Spectrum (2007)

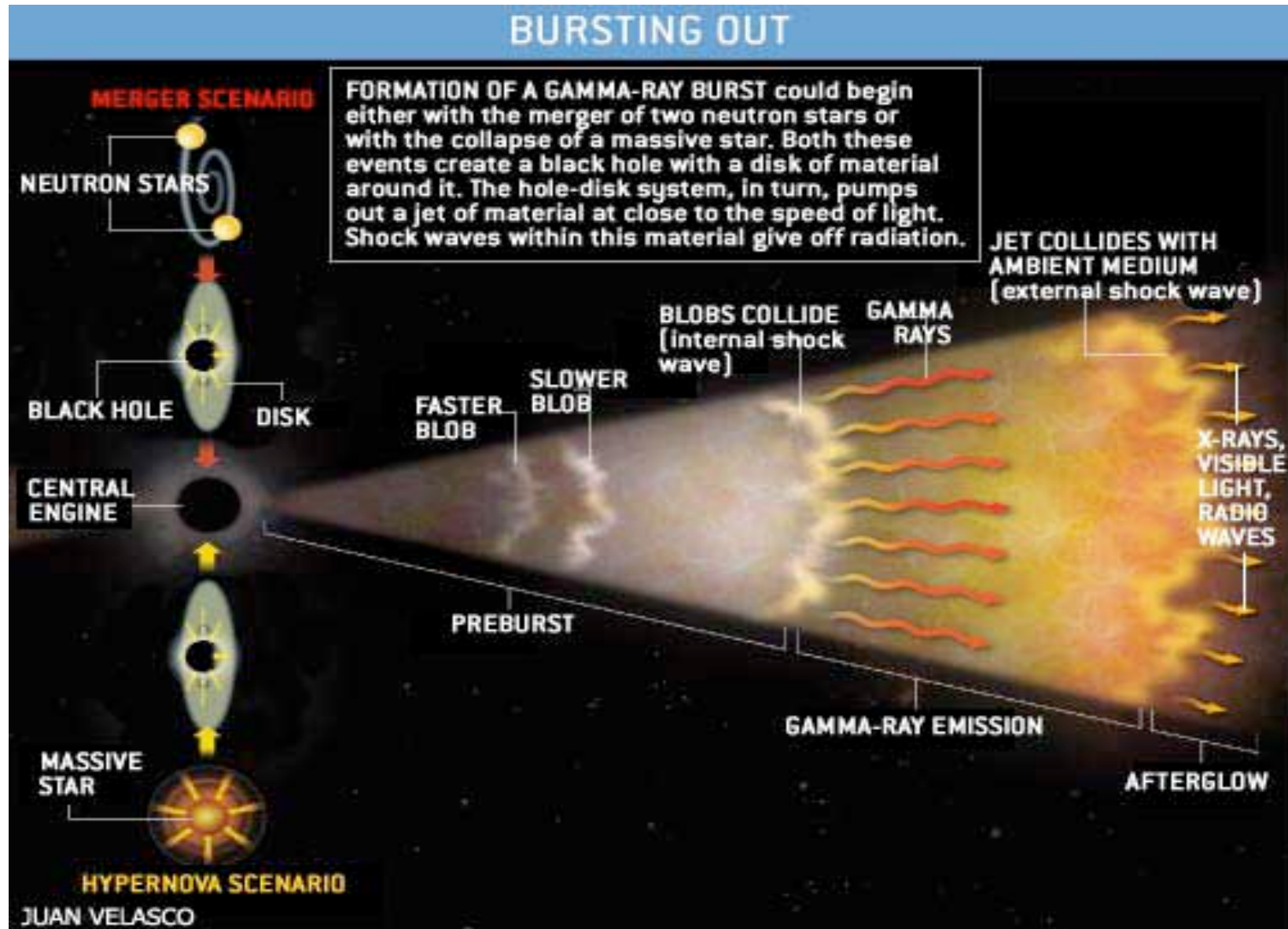


- Pierre Auger Array determination of UHECR spectrum ( $\times E^{2.6}$  above) *reveals GZK turnover* at 60 EeV (Roth et al. 2007).
- Confirms Fly's Eye and later Hires observations; contradicts AGASA results;
- $\Rightarrow$  UHECR sources must be further than around 30-50 Mpc.

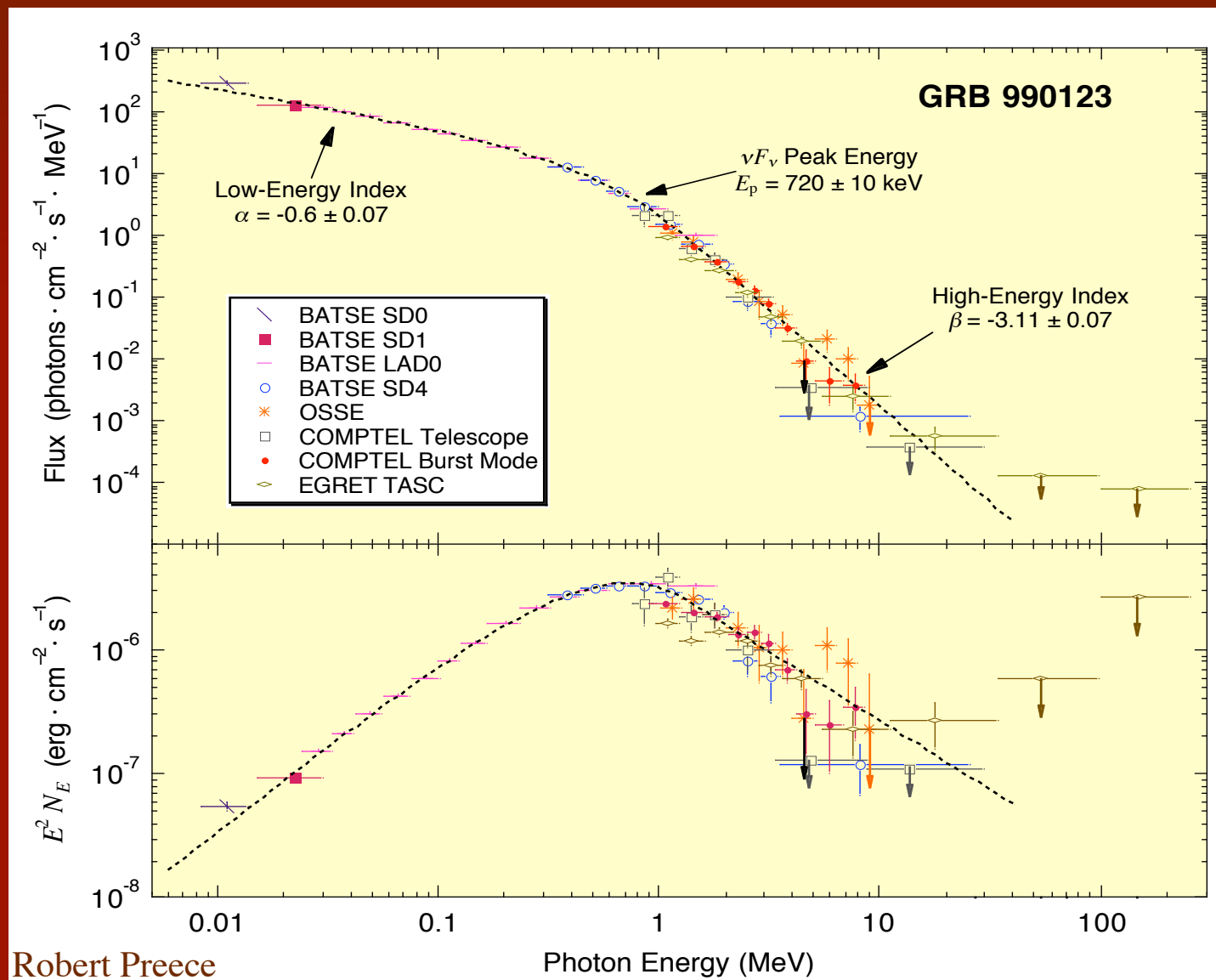
# BATSE Gamma-Ray Burst Lightcurves



# Gamma-Ray Bursts: Relativistic Outflows

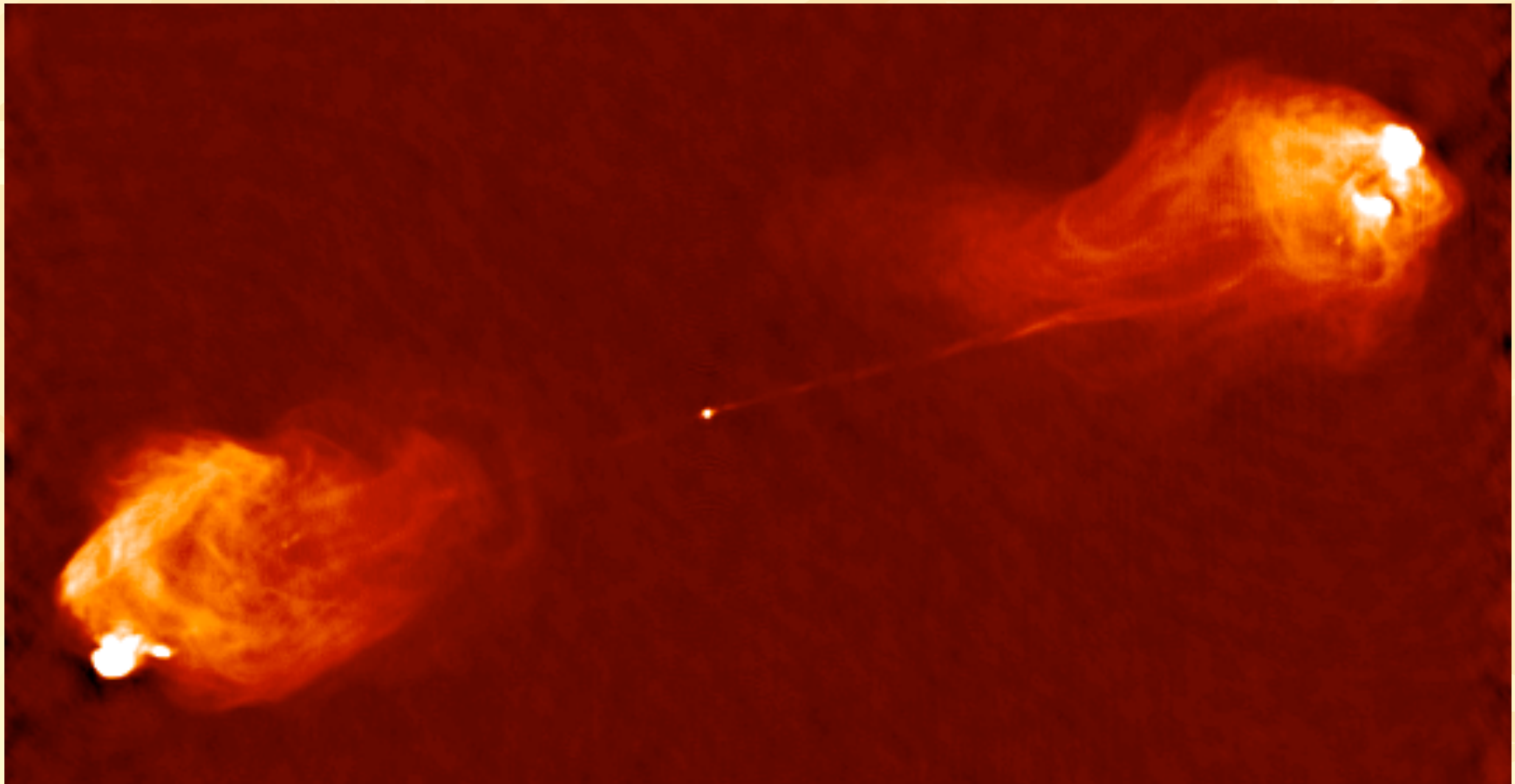


# Spectral Character: GRB990123



Credit: Robert Preece

# High Energy Cosmic Ray Accelerators: Radio Galaxies like Cygnus A

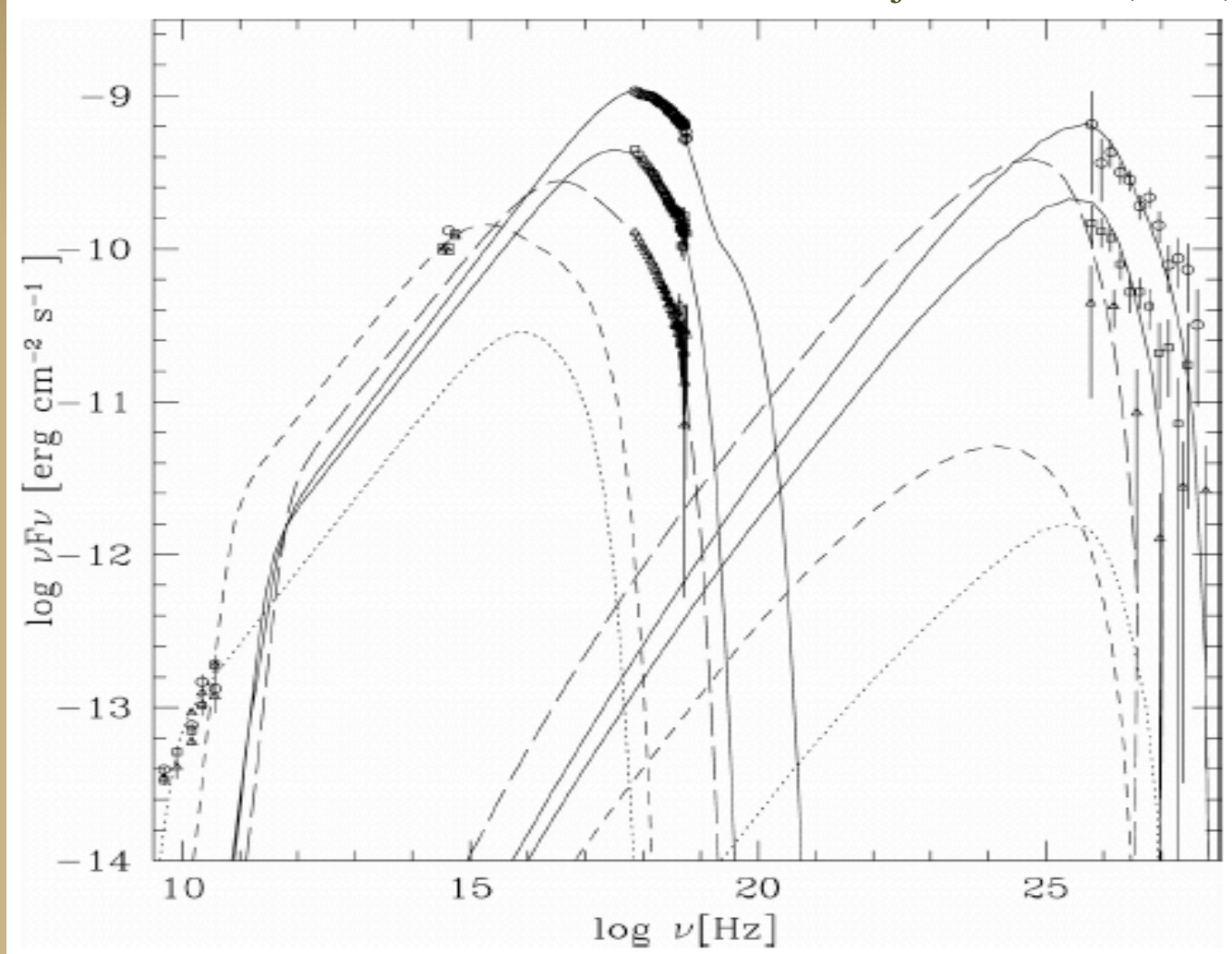




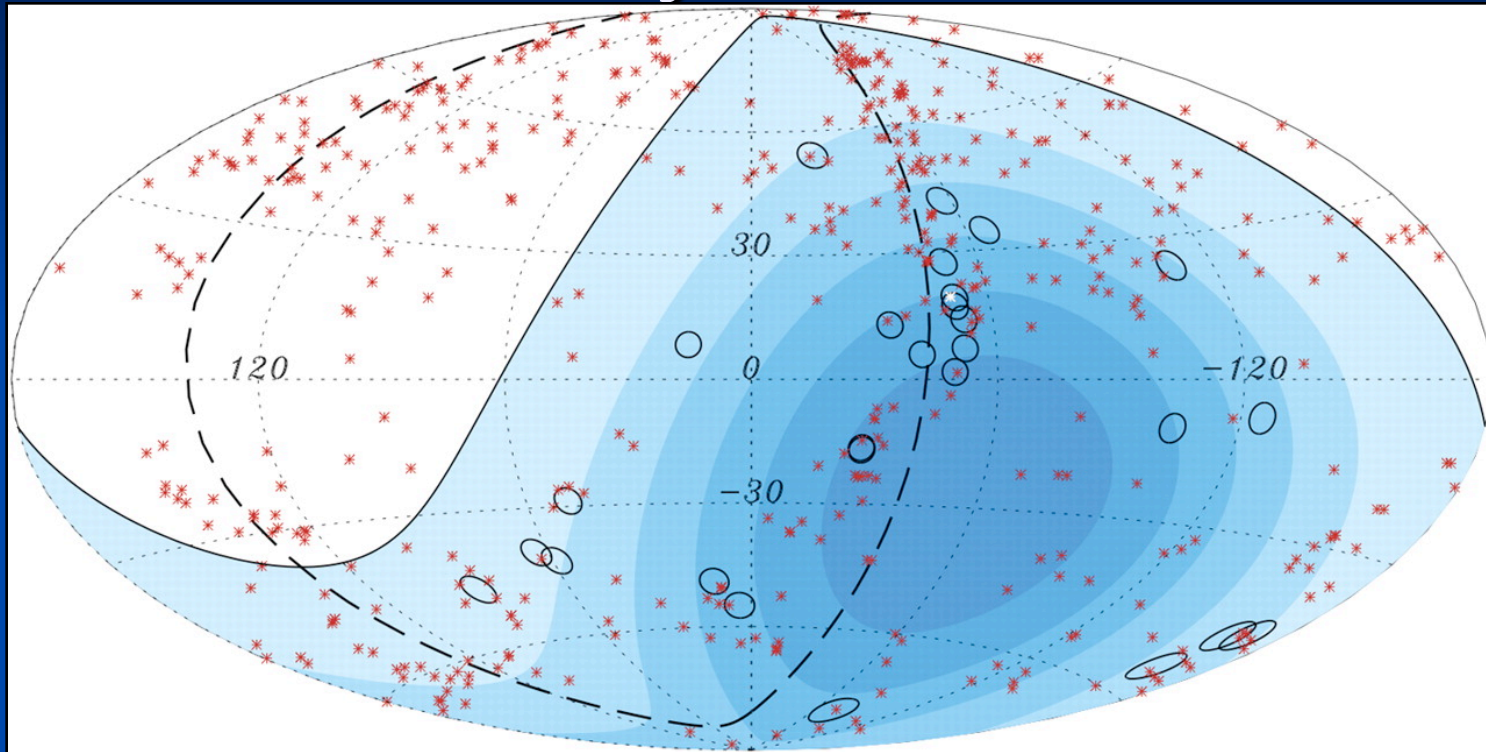
# Multi-wavelength Flaring in the Blazar Markarian 421

$z=0.031$

Blazejowski et al. (2005)



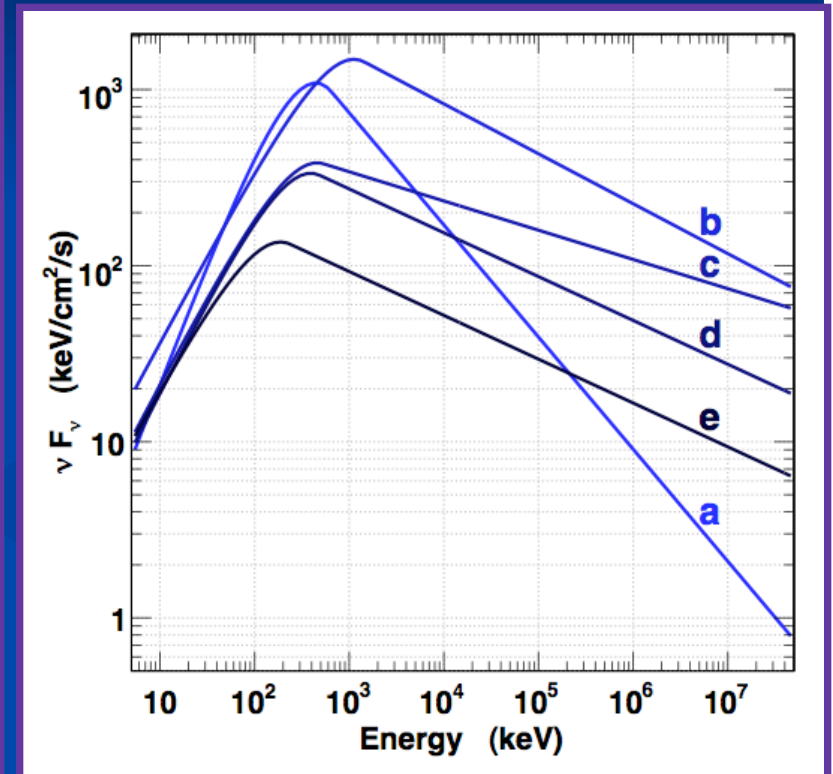
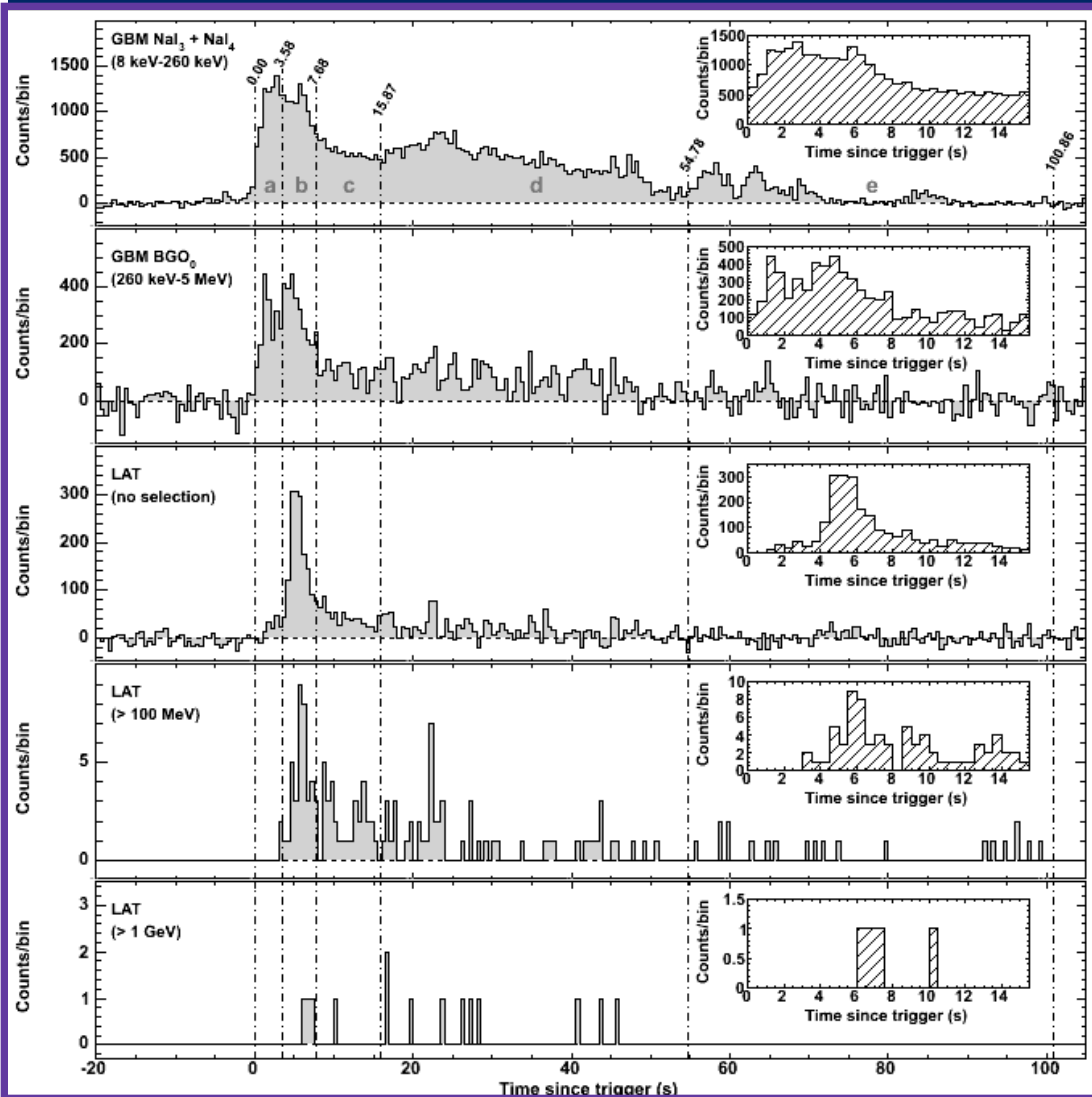
# Correlation of UHECR Directions with nearby ( $z < 0.02$ ) AGNs



- **Science (2007) 318, 938:** Pierre Auger Collaboration announces correlation of arrival directions on Celestial Sphere (Aitoff proj.) of the 27 cosmic rays (1.2 year's data) with highest energy ( $E > 57 \text{ EeV}$ ) with the positions of the 472 AGN (318 in the field of view of the Observatory) with redshift  $z < 0.018$  ( $D < 75 \text{ Mpc}$  Veron-Cetty 2006 catalog). The dashed line marks the Supergalactic plane.

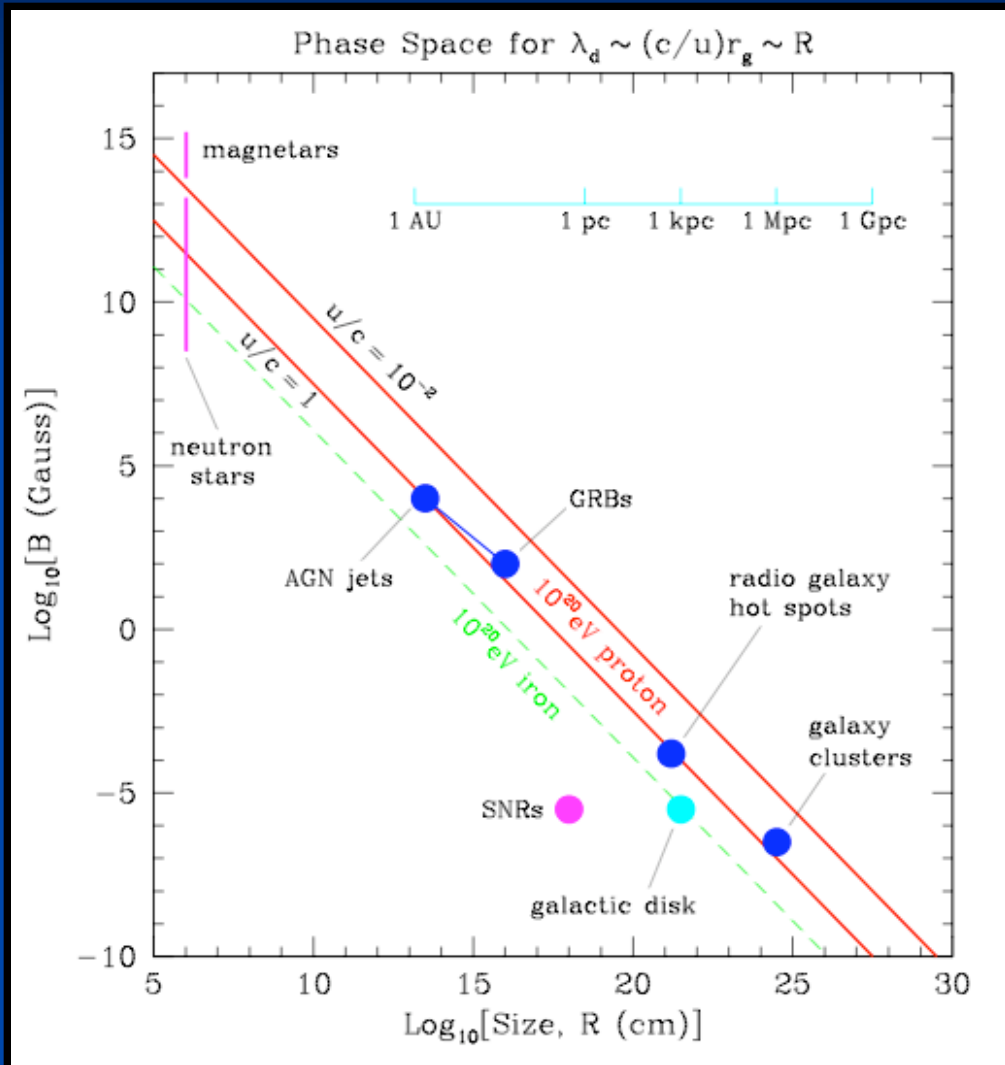
# Fermi GRB 080916c

## Temporal and Spectral Evolution



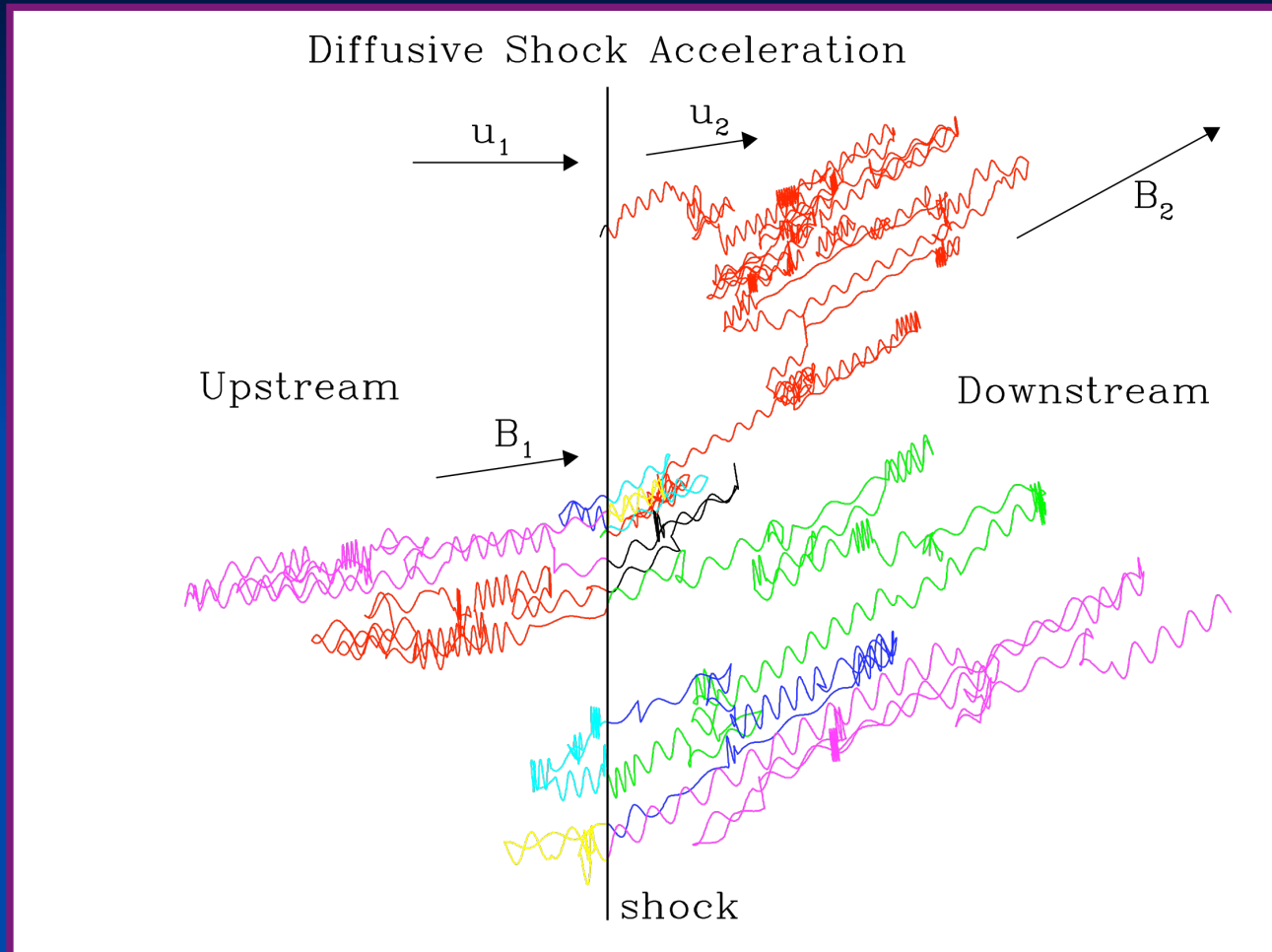
■ Science (2009):  
Abdo et al.

# Cosmic Ray Acceleration: Fields and Spatial Scales



- B-R phase space - after [Hillas \(1984\)](#);
- Based on diffusion theory at non-rel. shock using Bohm limit (mfp  $\lambda \sim c r_g / u$ );
- **Gyroresonant interactions operate;**
- AGN jets, GRBs and magnetars are best candidates for UHECR production.

# Monte Carlo Simulation Particle Trajectories

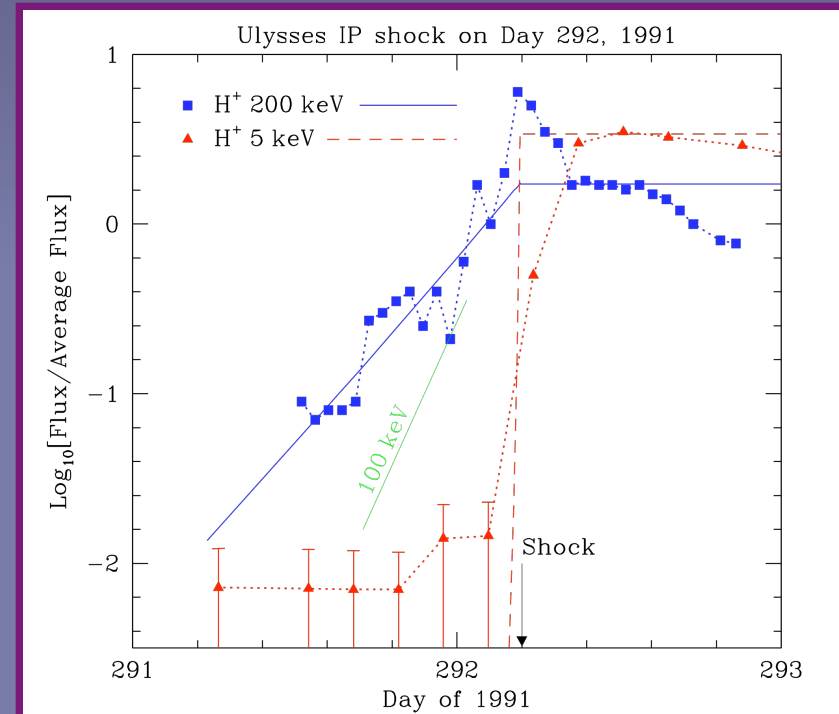
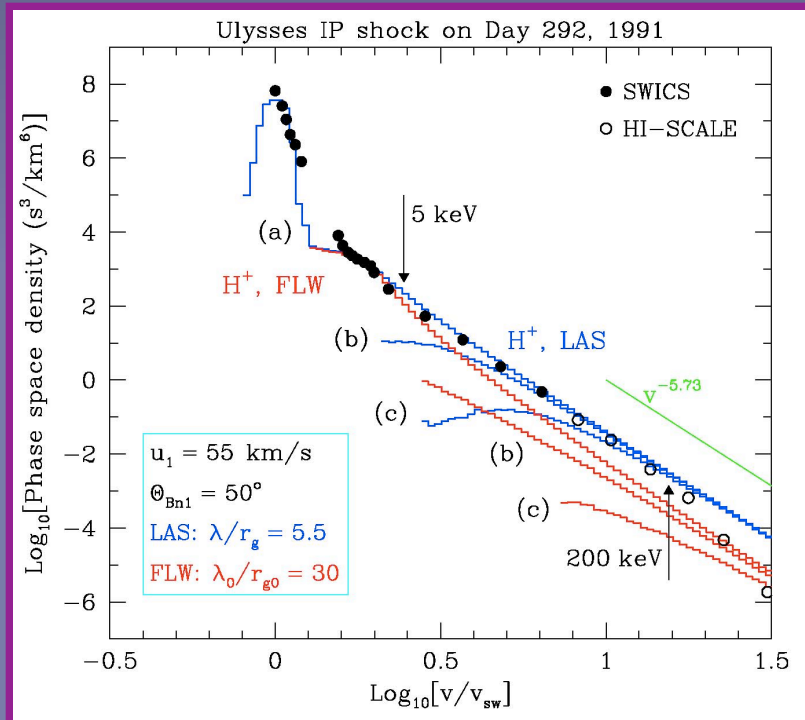


- Gyration in B-fields and diffusive transport modeled by a Monte Carlo technique; color-coded in Figure according to fluid frame energy.
- Shock crossings produce net energy gains (evident in the increase of gyroradii) according to principle of first-order Fermi mechanism.

# Shock Acceleration: Monte Carlo Simulations

- The Monte Carlo simulations use a **kinetic description of convection and diffusion** in MHD shocks (after Bell 1978);
- Thermal ions and  $e^-$  are injected far upstream of shock;
- **Particle diffusion in MHD turbulence** is phenomenologically described via the mean free path  $\lambda$  being some power of its gyroradius  $r_g$ : same prescription for both thermal and non-thermal particles, and for electrons and protons;
- Principal advantages include **addressing large momentum ranges** => **excellent for astrophysical problems**.
- **Simulations are fully relativistic**, and not restricted to subluminal shocks, and include shock drift acceleration;
- Technique has been **well-tested in heliospheric contexts** of acceleration at the **Earth's bow shock** (Ellison et al. 1990) and **interplanetary shocks** (Baring et al. 1997; Summerlin & Baring 2006) **using in-situ spacecraft data**.

# Ulysses 1991 Day 292 Shock: Spectral and Spatial Comparison



- **Left Panel:** Ulysses SWICS and HI-SCALE downstream data from Gloeckler, et al. (1994), together with MC simulation fit (upper blue histogram) to data from **Baring & Summerlin (2008)**.
- **Right Panel:** Spatial/temporal profiles for 5 keV (SWICS) and 200 keV (HI-SCALE) protons. MC model for LAS in strong field turbulence matches 200 keV ramp scale *for same turbulence parameter  $\lambda r_g$  that fits downstream spectrum.*

# Expectation Uncertainties for UHECRs

- Population statistics + source energetics:
  - Space distribution of source population;
  - Duty cycle of transient or flaring sources;
  - Non-thermal hadronic luminosity distribution function of candidate sources (i.e. AGNs and GRBs);
  - Relativistic beaming reductions of intrinsic source luminosity;
- Spectral form: power-law “lever arm” critical to fluxes predicted in *HIRES/Auger/AGASA* window;
  - shock acceleration expectations;
  - Tying cosmic ray spectra to candidate source gamma-ray spectra - a central role for *Fermi* science;
- Hadronic vs. leptonic acceleration efficiency:
  - non-thermal population abundances possess the biggest uncertainty: they are products of the acceleration environment.





# Spectral Properties of Diffusive Relativistic Shock Acceleration

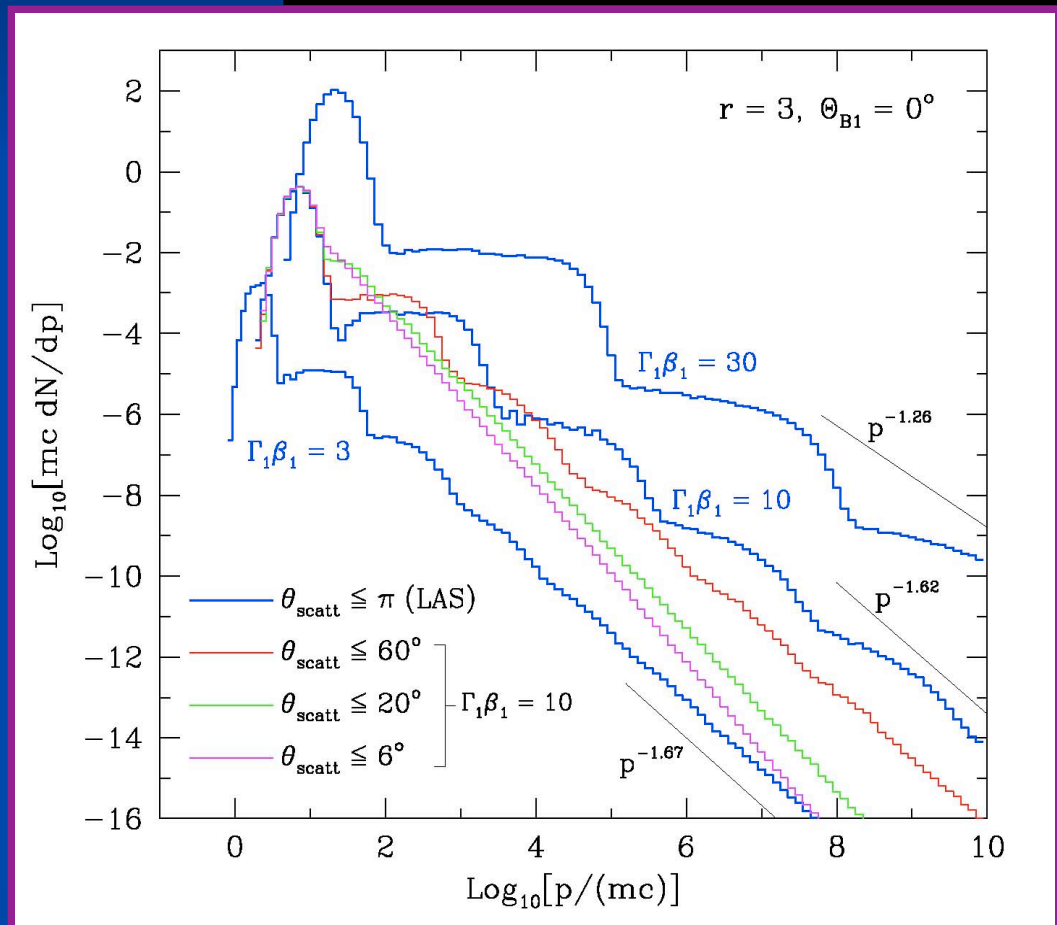
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- For small angle scattering, ultra-relativistic, parallel shocks have a power-law index of **2.23** (Kirk et al. 2000);
- Result obtained from solution of diffusion/convection equation and also Monte Carlo simulations (Bednarz & Ostrowski 1996; Baring 1999; Ellison & Double 2004);
- Power-law index is **not universal**: scattering angles larger than Lorentz cone flatten distribution;
- Large angle scattering yields kinematic spectral structure;
- Spectral index is generally (but not always) a strongly *increasing* function of field obliquity angle  $\Theta_{Bn1}$ .

# Relativistic Shocks: Spectral Dependence on Scattering

- Deviations from “canonical” index of 2.23 (Bednarz & Ostrowski 1998; Kirk et al. 2000; Baring 1999) occur for scattering angles  $> 1/\Gamma_1$ , i.e. *outside Lorentz cone*;
- Large angle scattering yields kinematically structured distributions;
- (e.g., Ellison, Jones & Reynolds 1990; Ellison & Double 2004; Baring 2005)

Stecker, Baring & Summerlin 2007



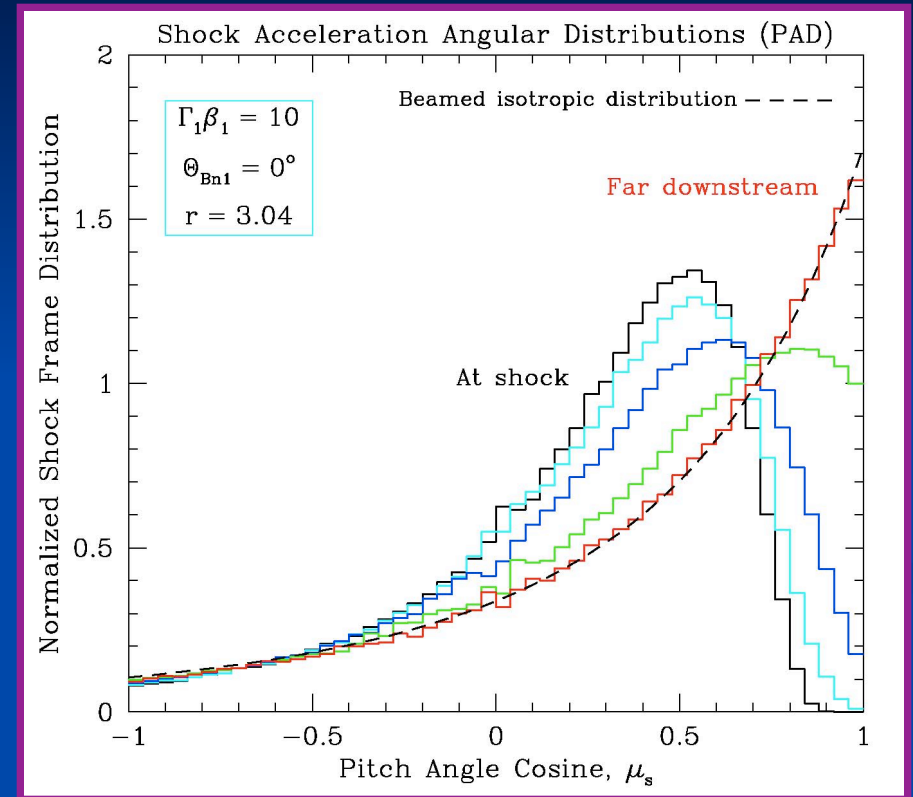
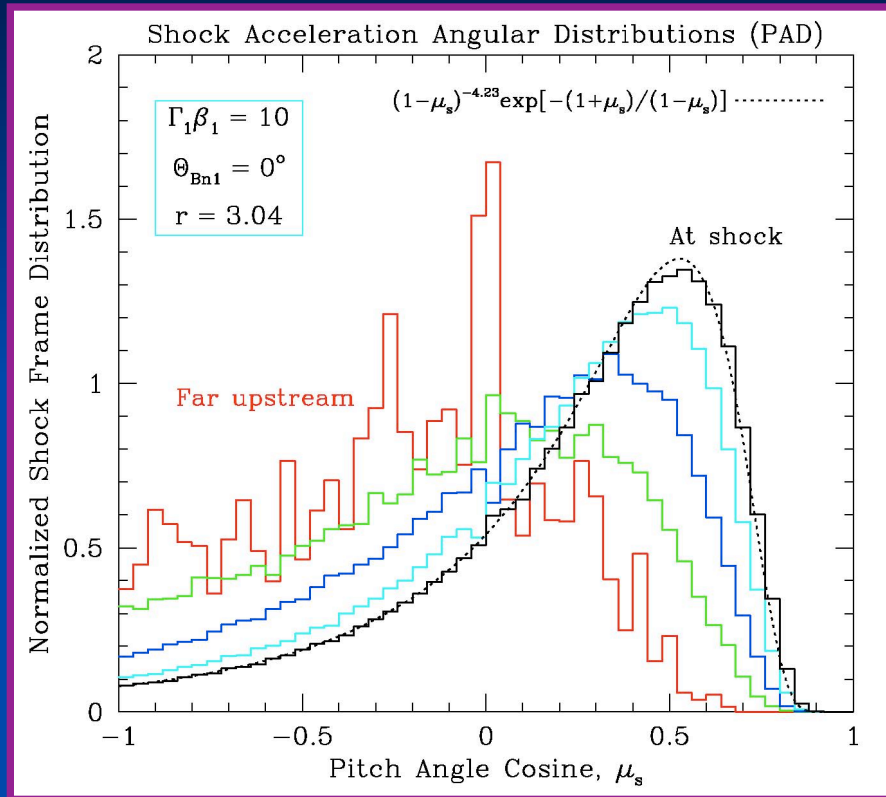


# The Character of Relativistic Shocks

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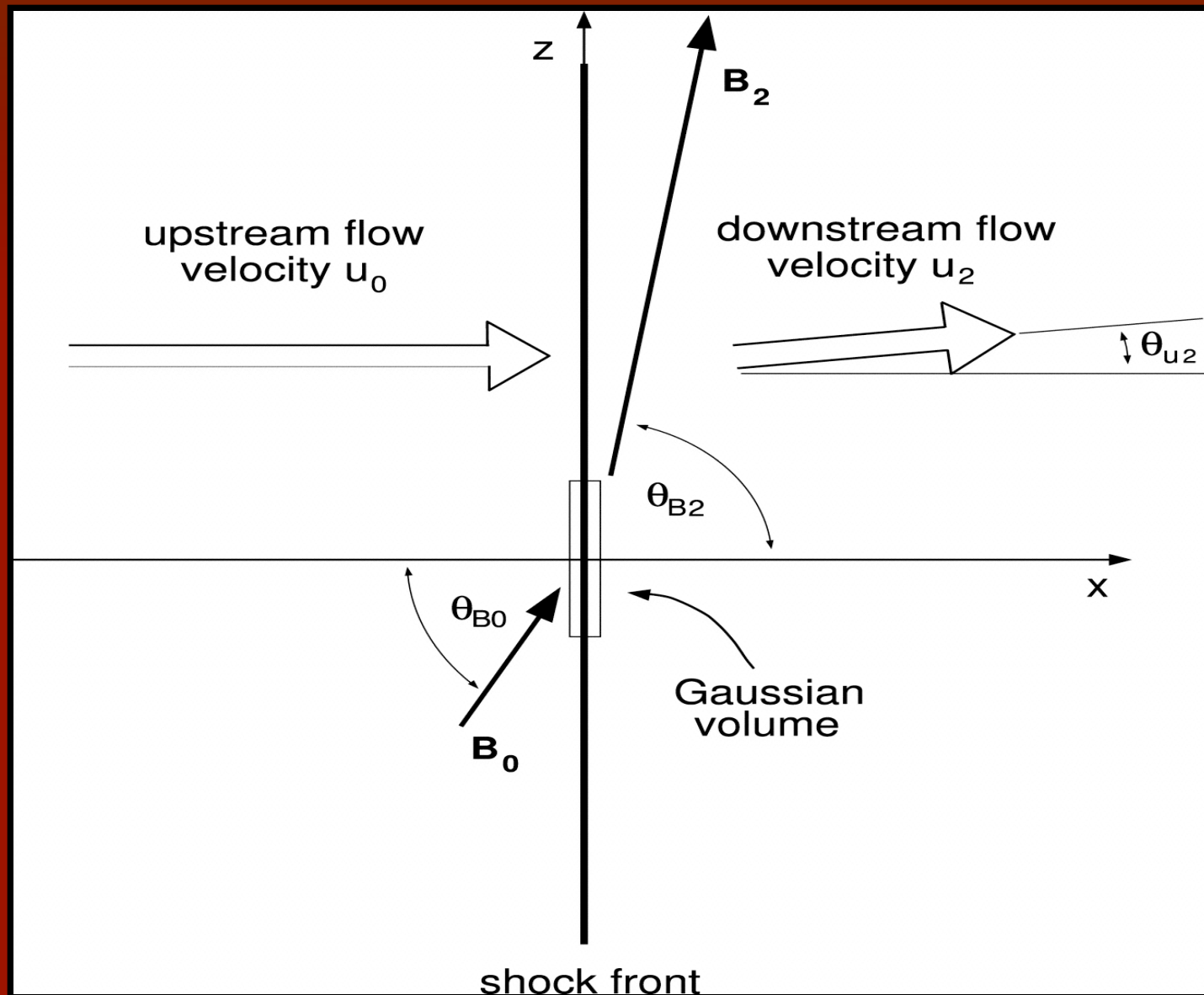
- Character of relativistic shocks defined by their **intrinsic anisotropy**: convective influence is profound, particularly for superluminal cases;
- Escape downstream is a ***strong function*** of **shock speed and field obliquity**: convective loss rates are high;
- Acceleration times are not modified strongly by relativistic effects (EJR90, Baring 2002).

# Upstream and Downstream Angular Distributions

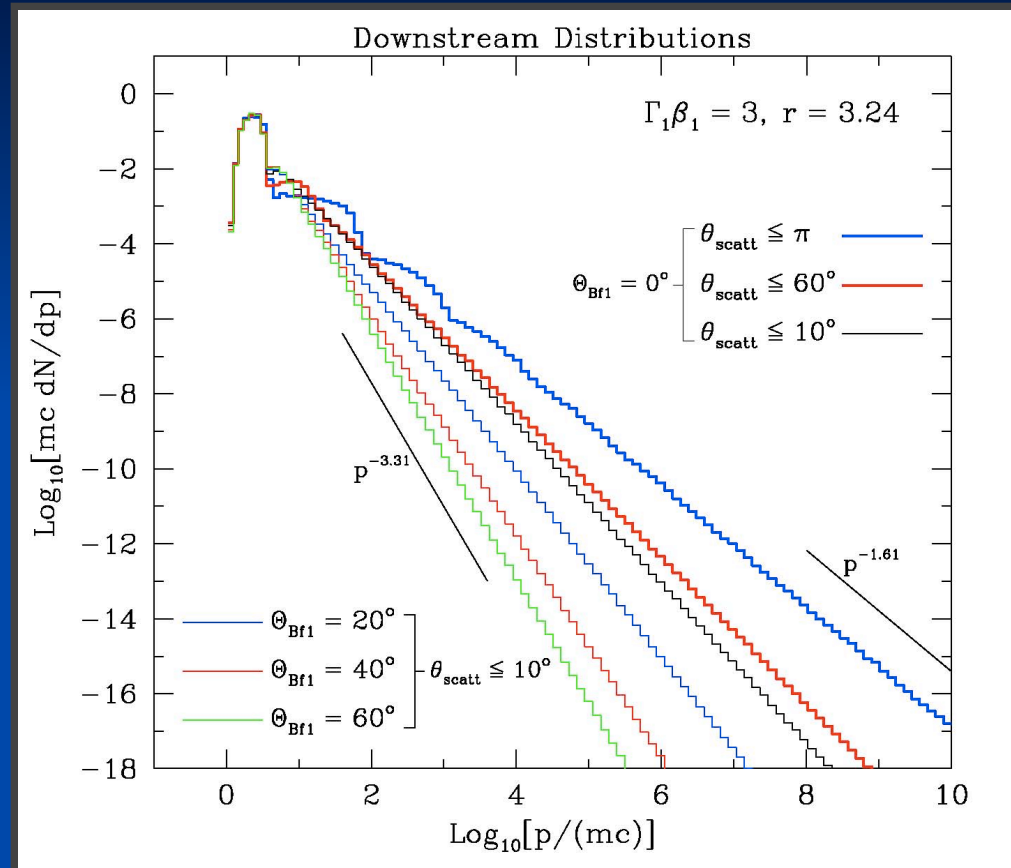


- **Pitch angle diffusion (PAD)** simulation shock frame distributions for a parallel, relativistic shock with  $\Gamma_1\beta_1=10$ .
- *Left Panel*: different distances upstream. At the shock (black), simulation results closely approximate the asymptotic ( $\Gamma_1\beta_1 \gg 1$ ) analytic form of [Kirk et al. \(2000\)](#).
- *Right Panel*: different distances downstream of the shock. Far downstream, the distribution approximates that for an isotropic fluid boosted by  $\beta_2=1/3$ .

# Oblique Shock Geometry



# Spectral Dependence on Field Obliquity

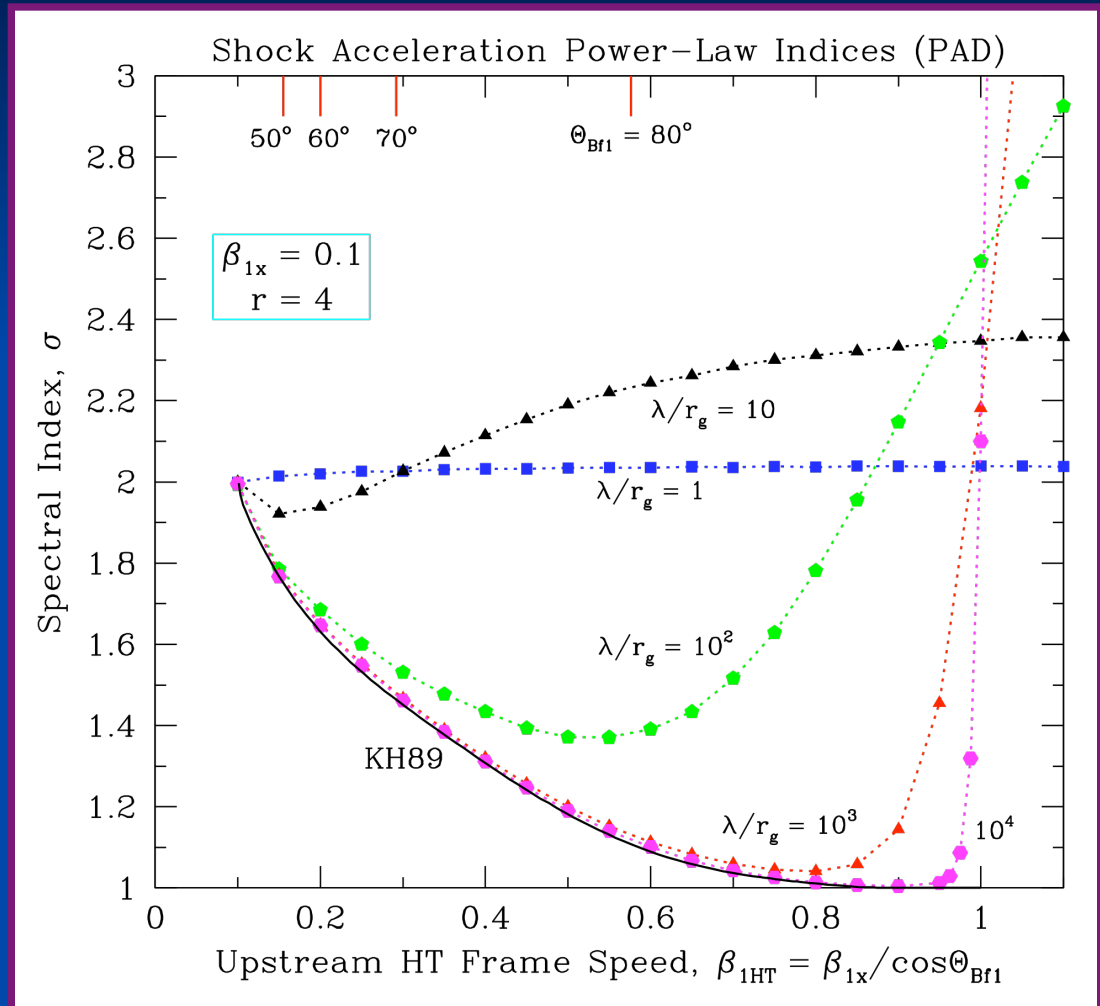


Superluminal  
Cases ->

- Increasing upstream B-field obliquity and/or ratio of mean free path to gyroradius steepens the continuum (e.g. Bednarz & Ostrowski 1998; Ellison & Double 2004; Summerlin & Baring 2009 [in prep]; Kirk & Heavens 1989).

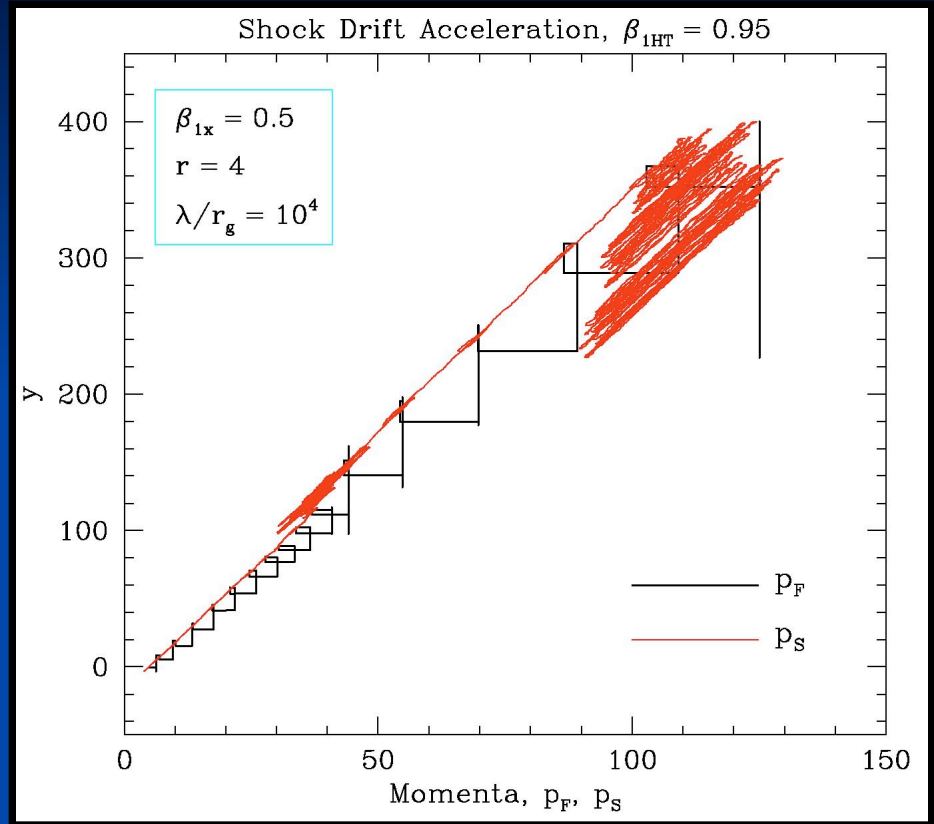
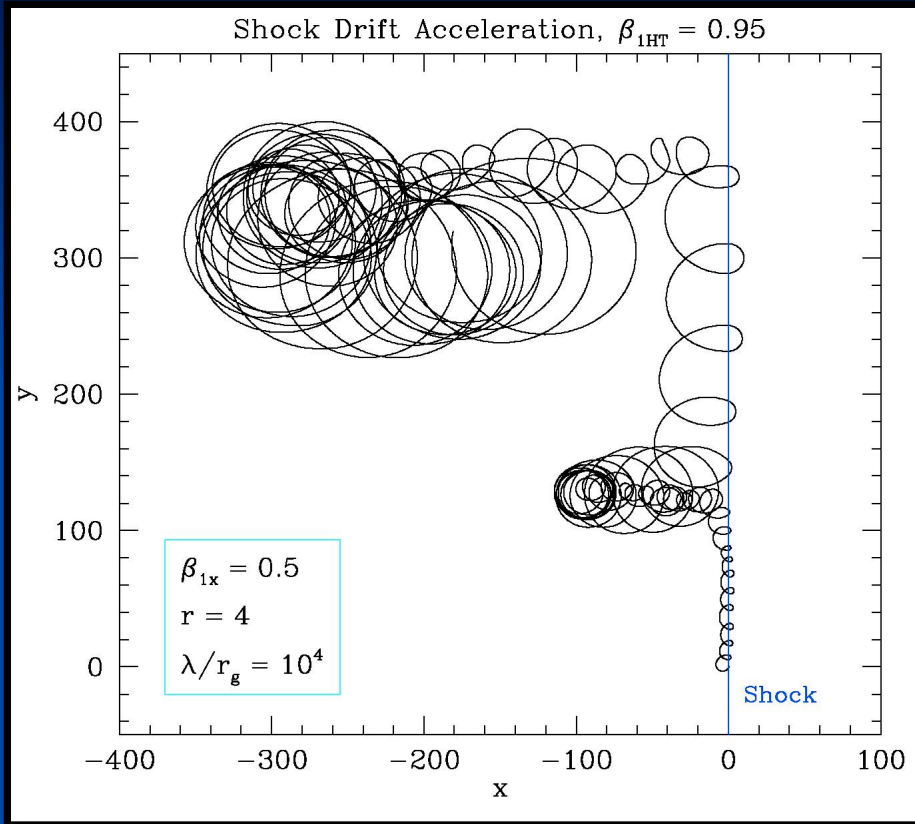
# Shock Acceleration Spectral Indices

- To compare with Kirk & Heavens (1989) solutions of convection-diffusion equation (oblique shocks).
- Power-law indices in the limit of small angle scattering (pitch angle diffusion: PAD) **range considerably**;
- For absolutely no cross field diffusion ( $\lambda/r_g \rightarrow \infty$ ), the index is **as low as unity** and the distribution is extremely flat:
- Such regimes correspond to **pure shock drift acceleration**, and are **extremely unlikely**.



Baring & Summerlin 2009, in prep.

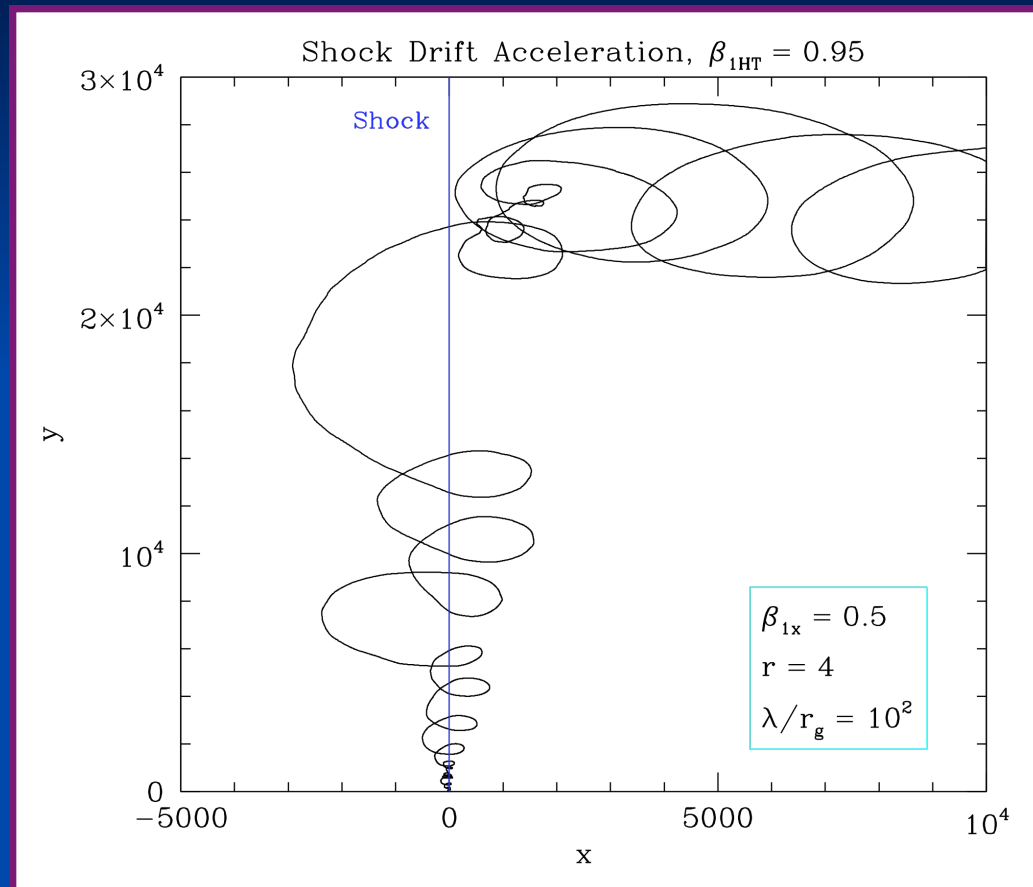
# Shock Drift in Action: $\lambda/r_g = 10^4$



- *Left Panel*: projection of a selected ion orbit onto the x-y plane, exhibiting drifting in the shock layer. *Right Panel*: evolution of magnitudes of momentum in fluid ( $p_F$ ) and shock ( $p_S$ ) frames versus  $y$ , indicating shock drift episodes interspersed with upstream diffusive hiatuses in energy gain;
- Lowering  $\lambda/r_g$  rapidly degrades the contribution of shock drift, enables particle convection downstream, and steepens spectrum.



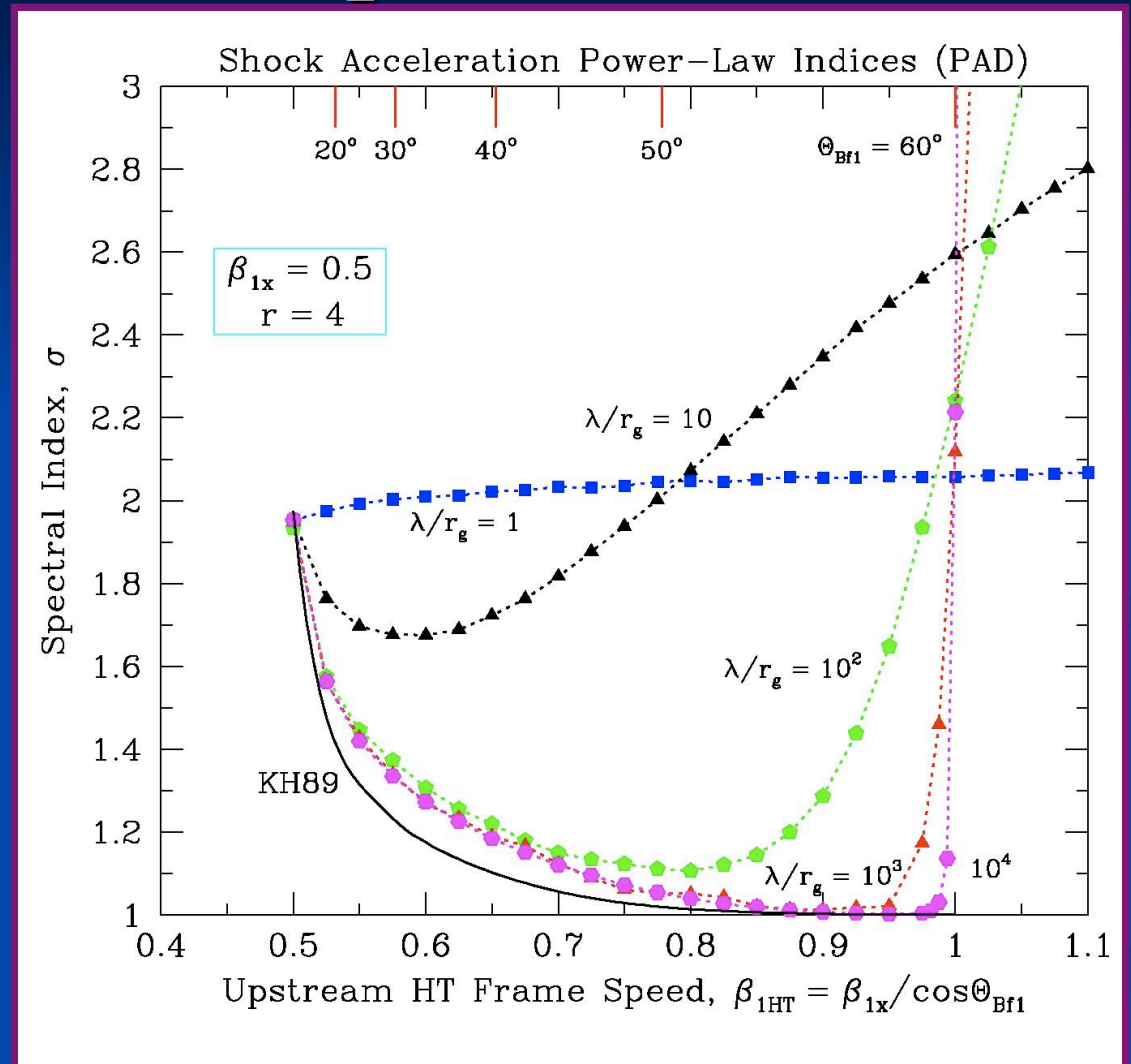
# Disrupted Shock Drift: $\lambda/r_g = 10^2$



- Projection of a selected ion orbit onto the x-y plane, exhibiting drifting in the shock layer. Exhibits “wonky drift.”
- Lowering  $\lambda/r_g$  rapidly degrades the contribution of shock drift, enables particle convection downstream, and steepens spectrum.

# Shock Acceleration Spectral Indices

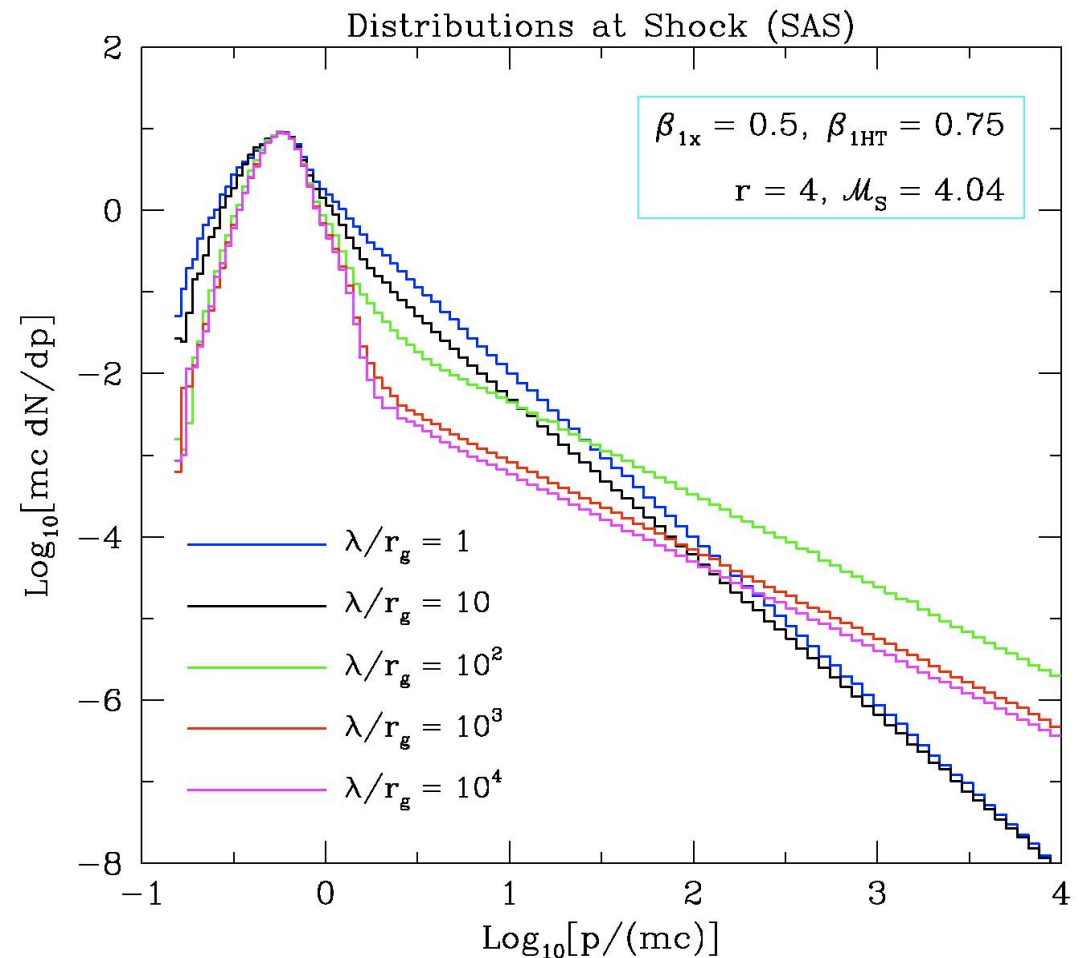
- Power-law indices in the limit of small angle scattering (pitch angle diffusion: PAD) **range considerably**;
- In cases of absolutely no cross field diffusion, the index is **as low as unity** and the distribution is extremely flat;
- Gyro-orbit simulations for  $\lambda/r_g \rightarrow \infty$  do not quite match Kirk & Heavens (1989, KH89) solutions to diffusion-convection equation, since **KH89 assumes conservation of adiabatic moment** for particles interacting with the shock.



Baring & Summerlin 2009, in prep.

# Shock Acceleration Injection Efficiencies

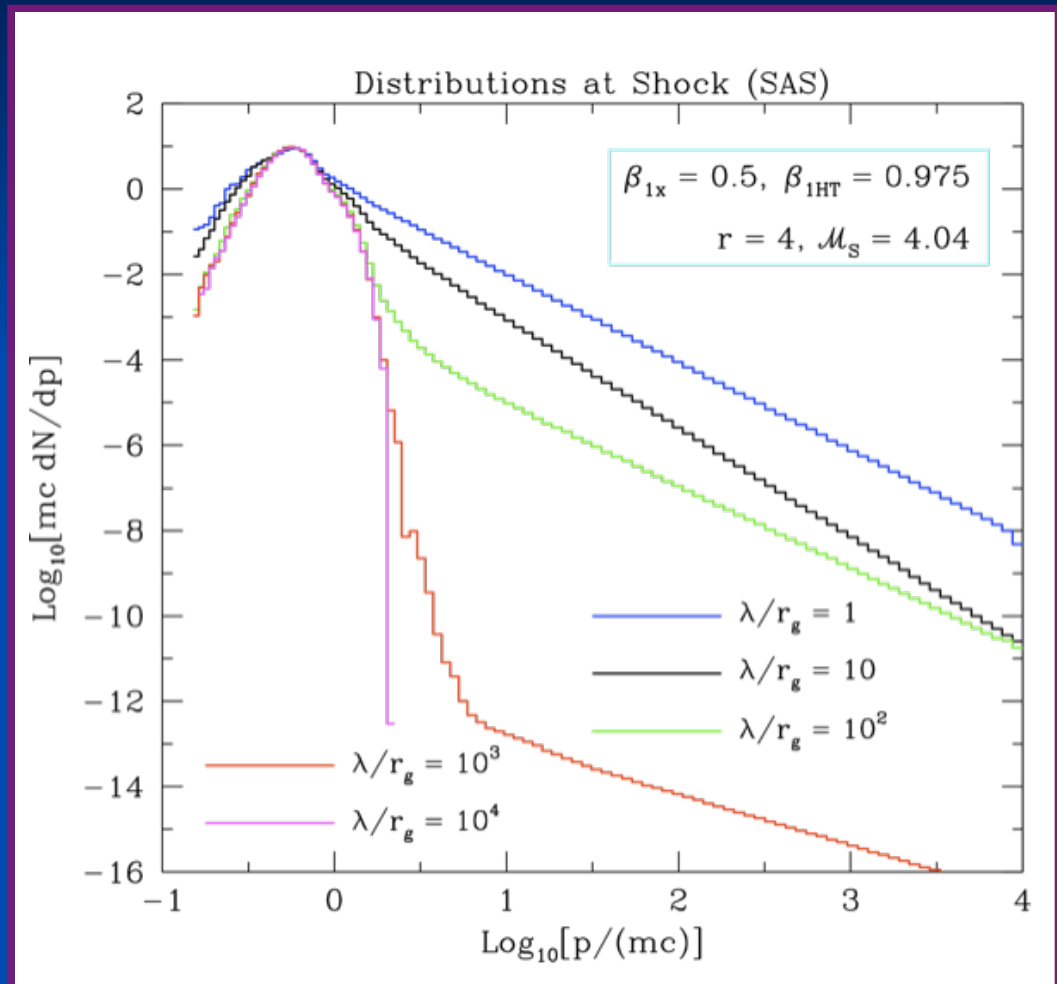
- Complete particle spectra in the limit of small angle scattering (pitch angle diffusion: PAD) **range considerably**;
- In cases of strong cross field diffusion, the index is **around two** and the injection is efficient;
- Gyro-orbit simulations for  $\lambda/r_g \rightarrow \infty$  that give flat power-law indices are poor injectors – this becomes far more extreme as HT frame speed approaches  $c$ .



Baring & Summerlin 2009, in prep.

# Injection Efficiencies: Near Luminality

- When shocks are nearly luminal, the injection efficiency precipitously drops in gyro-orbit simulations as  $\lambda/r_g \rightarrow \infty$ .
- $\Rightarrow$  flat power-law index cases are poor injectors – this becomes far more extreme as HT frame speed approaches  $c$ .
- Rapid convection downstream inhibits suprathermal injection.
- Stochastic heating can aid injection: only modestly.
- Astrophysical requirements of moderate turbulence and injection efficiency advocate spectra steeper than  $E^{-1.5}$ .



Baring & Summerlin 2009, in prep.

# Implications for sources of UHECRs

- Relativistic shocks can generate a multitude of spectral forms: power-law indices depend on shock parameters and scattering properties;
- => **Non-canonical spectral index**
- Distinct contrast to non-relativistic case [depends on  $r$  only];
- Spectrum is only flat for quasi-parallel shocks *or* strong turbulence, **if shocks are superluminal**;
- GRB prompt and afterglow emission more easily explained by *mildly-relativistic shocks* that are *not quasi-perpendicular* (for diffusive acceleration scenarios). True also perhaps for radio galaxies.

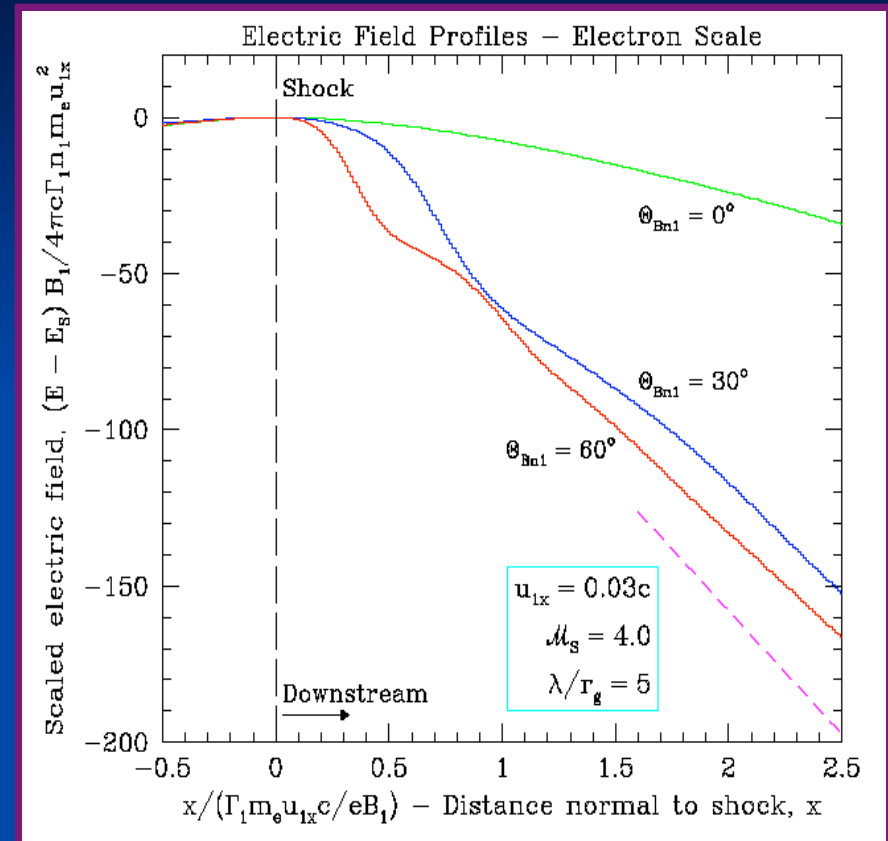
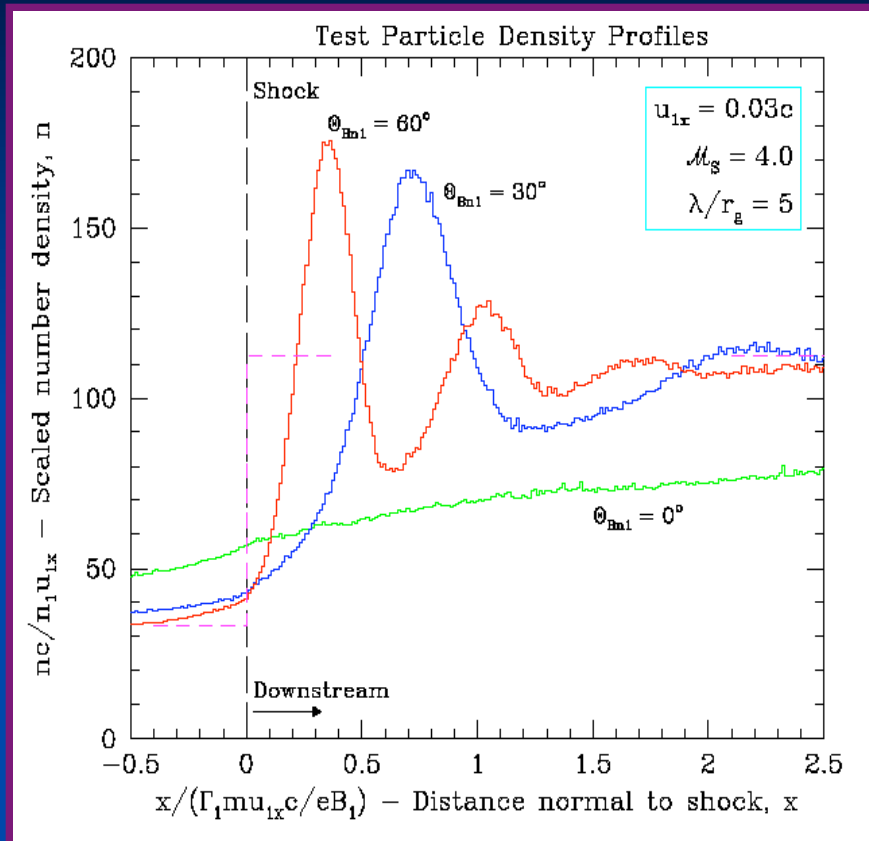
# Conclusions

- Shock acceleration particle spectral indices depend on several shock parameters: **field obliquity** to the shock normal, **scattering strength** or level of MHD turbulence, **amount of diffusion across B**; => **there is no canonical spectral index.**
- Unless source shocks are superluminal and only modestly turbulent, UHECR spectral generation is easily realized for a variety of conditions in relativistic shocks.
- The  $e-p$  abundance ratio, a key parameter for the UHECR and neutrino cosmic flux budget, is still a critical unknown – a goal for future simulation probes.
- GRB and AGN spectra are intimately connected to detailed shock parameters => *Fermi* role for gamma-ray spectral diagnostics for both hadronic and leptonic models.
- **Extremely flat spectra can be realized in sub-luminal shocks with minimal cross field diffusion:** efficient retention of particles in the shock layer permits efficient action of shock drift acceleration.
  - **Unlikely to be realized in Nature! And not commensurate with source photon signals.**

# Power-Law Normalizations: the big Unknown

- For single component species, the downstream thermal population is **heated to momentum  $\sim \Gamma_1 \beta_1 mc$** . This effectively establishes the power-law normalization;
- For relativistic  $e$ - $p$  shocks, this introduces a temperature ratio  $T_e/T_p \sim m_e/m_p$  that effects **a normalization ratio  $\varepsilon_e \sim (m_e/m_p)^\sigma$  of  $n_e/n_p$  in the power-law domain**;
- For  $\sigma \sim 2$ , **this offset is large:  $\varepsilon_e \sim 10^{-8}$** ;
- In most source modeling to date, this unknown is chosen.
- Need to consider:
  - the effect on  $\varepsilon_e$  by heating of thermal electrons in plasma shocks via  **$e$ - $p$  charge separation potentials** in the shock layer [  $e^+$ - $e^-$  pair shocks don't exhibit such separations ];
  - Turbulent heating modifications to  $\varepsilon_e$  in PIC simulations.
- **These can increase  $\varepsilon_e$  by several orders of magnitude.**
- Relevant both for UHECR and VHE neutrino flux budgets, as well as ***Fermi*** gamma-ray sources.

# Density and Electric Field Profiles - low $M_s$



(Density profiles apply to e or p)

- Heating the beam smooths out the gyrational influence on density and E-field profiles. Correlation of gyrational peaks with field obliquity is marked.
- Efficient acceleration in parallel shocks diminishes density compression on sub-diffusive scales (i.e.  $|x| < 5$  here).
- Dashed magenta lines mark Rankine-Hugoniot densities and (maximal) E.



# Shock Drift in Oblique, Non-Relativistic Systems

DECKER AND VLAHOS

(DV 1986)

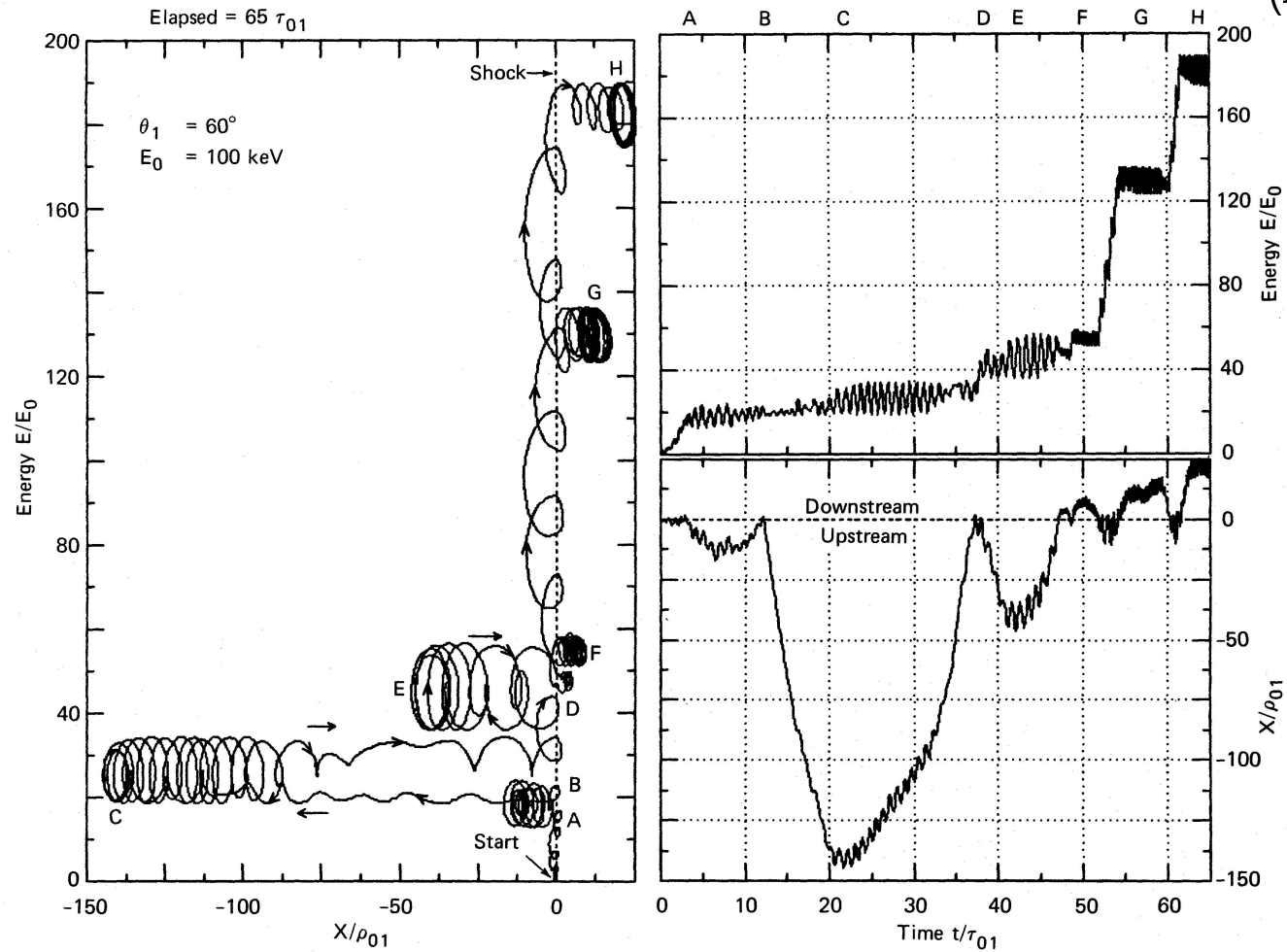
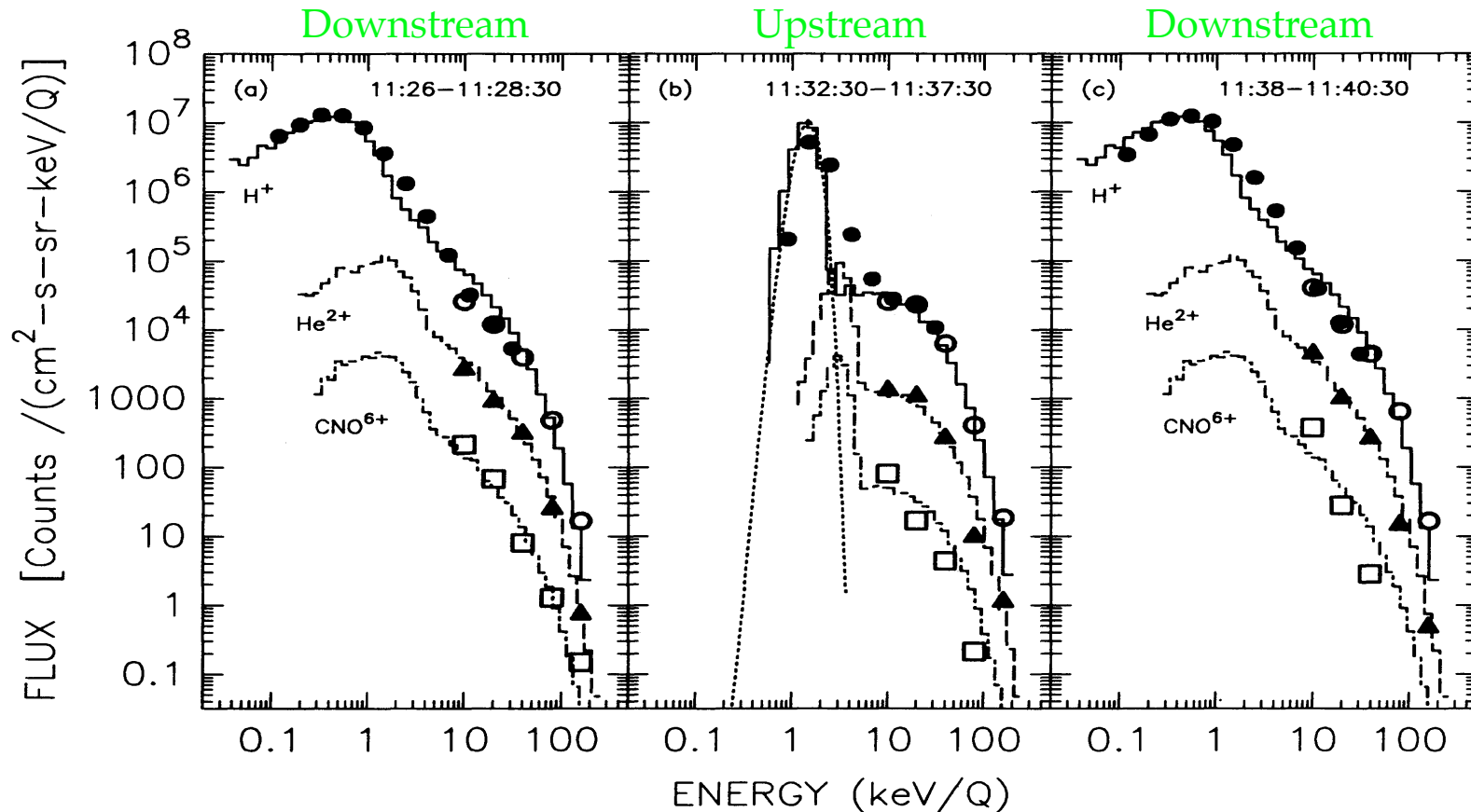


FIG. 6.—Sample for quasi-perpendicular shock  $\theta_1 = 60^\circ$ . See Fig. 5 caption and text for details.

# Ion Acceleration at Earth's Bow Shock

Ellison, Moebius & Paschmann (1990)



- AMPTE observations of diffuse ions at Q-parallel Earth bow shock **H<sup>+</sup>, He<sup>2+</sup> and CNO<sup>6+</sup>** observed during time when solar wind magnetic field was nearly radial;
- Efficient acceleration (25%) in high MS shock; model fits work only for non-linear model that exhibits A/Q enhancements; Scholer, Trattner & Kucharek (1992) found similar results with hybrid PIC simulations.

# Anisotropies in Relativistic Shocks: Pitch Angle Diffusion, $0.1c < u_1 < c$

Kirk, Guthmann, Gallant & Achterberg (2000)

