



# Dark Matter in the Universe

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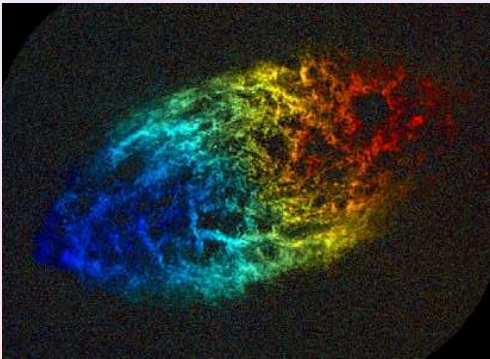
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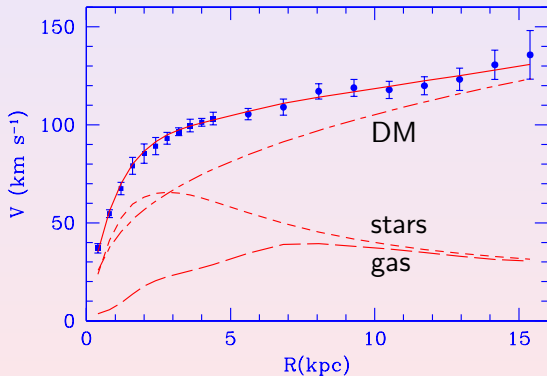
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# The standard lore:

- inflation suggests  $\Omega \equiv \rho/\rho_{\text{cr}} = 1$

$$H^2 \equiv \left(\frac{\dot{R}}{R}\right)^2 = \frac{8\pi}{3}G\rho - \frac{k}{R^2} + \frac{\Lambda}{3}$$

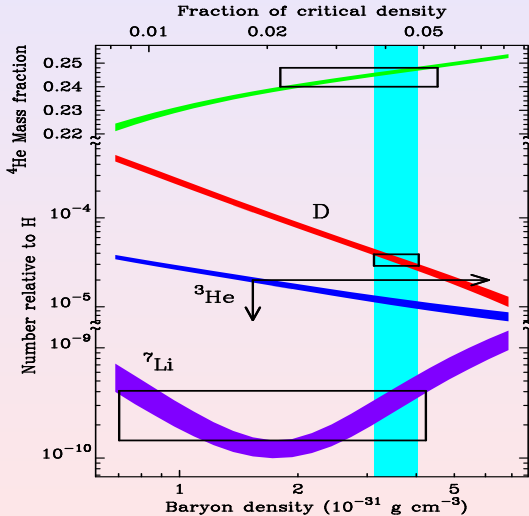
with  $\rho_{\text{cr}} = 3H_0^2/(8\pi G)$ :

During inflation

$$|(\Omega_{\text{tot}} - 1)| = \frac{k}{\dot{R}^2} \propto \exp(-2Ht)$$

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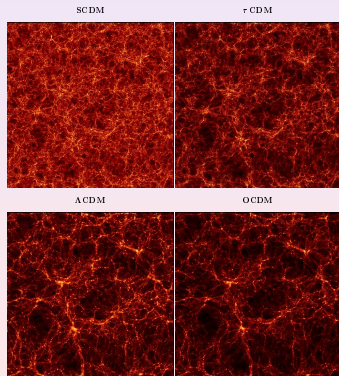




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  - “cold”, i.e. non-relativistic already for  $z_{\text{dec}} \lesssim z \lesssim z_{\text{eq}}$

$z=1$

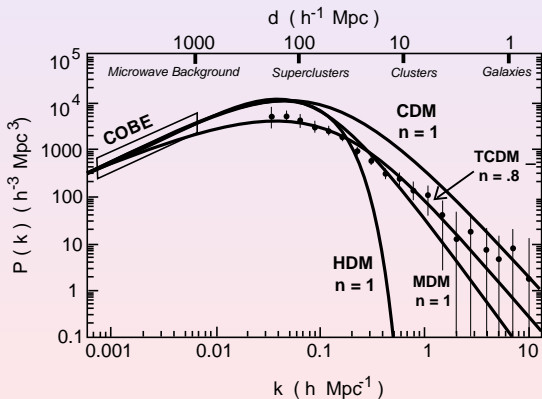


Jeans criterion:

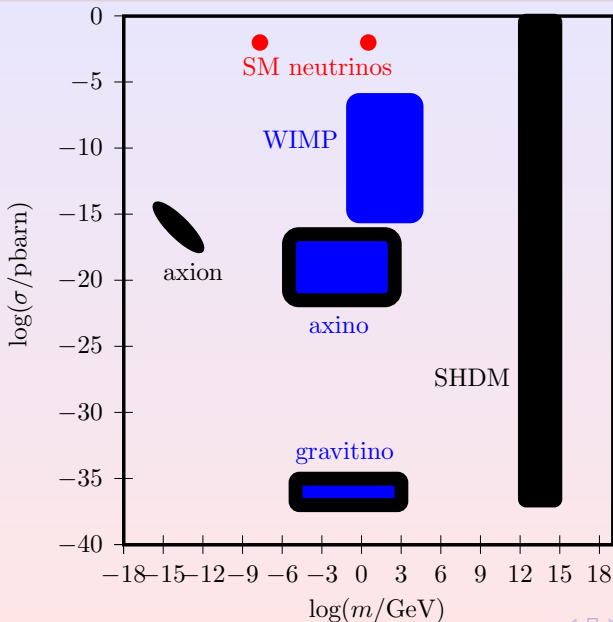
$$k_J = \left( \frac{4\pi G \rho_0}{v_s^2} \right)^{1/2}$$

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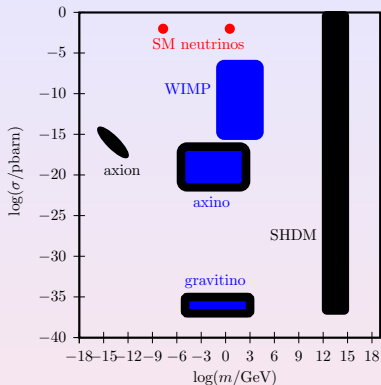
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why such a large variability? **Different production mechanism**

- thermal relics: WIMPs
- production in phase transitions: axions
- gravitational production: superheavy dark matter (SHDM)

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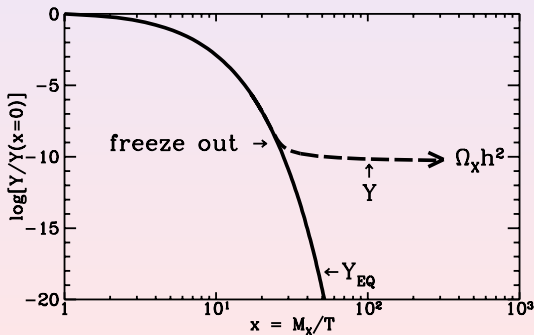
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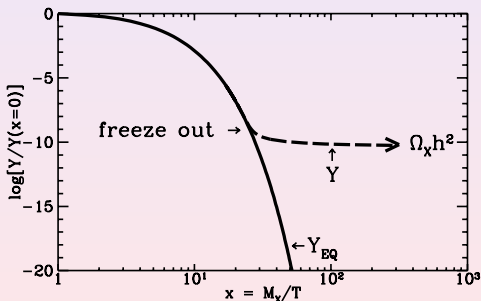
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$$\Omega_x h^2 \sim \frac{3 \times 10^{-26} \text{cm}^3/\text{s}}{\langle \sigma_{\text{ann}} v \rangle}$$

⇒ suggests weakly interacting DM particle with mass  $m \sim m_Z$



# Connection of $\Omega_X$ and $\langle\sigma_{\text{ann}}v\rangle$

- Gamov criterion

$$\Gamma_{\text{ann}} = n\langle\sigma_{\text{ann}}v\rangle \stackrel{!}{=} H = 1.66g_*^{1/2} \frac{T^2}{M_{\text{Pl}}}$$

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- thermally averaged annihilation cross section

$$\begin{aligned}\langle\sigma_{\text{ann}}v\rangle &= \sigma_0 + \sigma_1 v^2 + \sigma_2 v^4 + \dots \\ &= \sigma_0 + \tilde{\sigma}_1 T/m + \tilde{\sigma}_2 (T/m)^2 + \dots\end{aligned}$$

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- known value of  $\Omega_X$  fixes  $\sigma_0$  today



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- **Unitarity** of  $S$ -matrix restricts annihilations into  $l$ .th partial wave,

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- observed  $\Omega_{\text{CDM}} h^2 = 0.105 \propto 1/\langle \sigma_{\text{ann}} v \rangle \Rightarrow$

$$M_X \lesssim 35 \text{ TeV}$$

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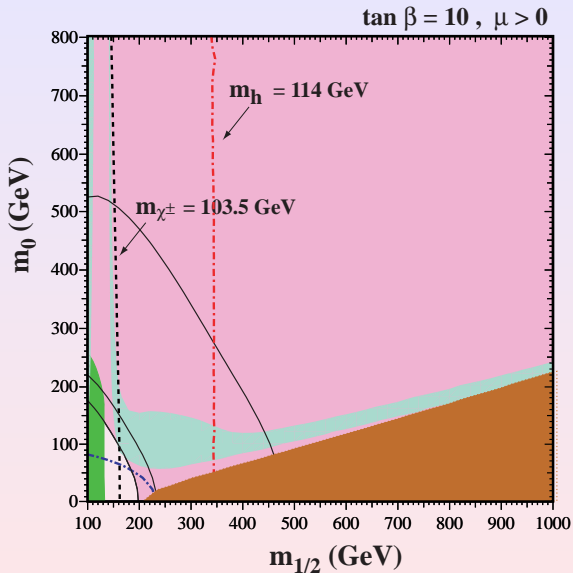
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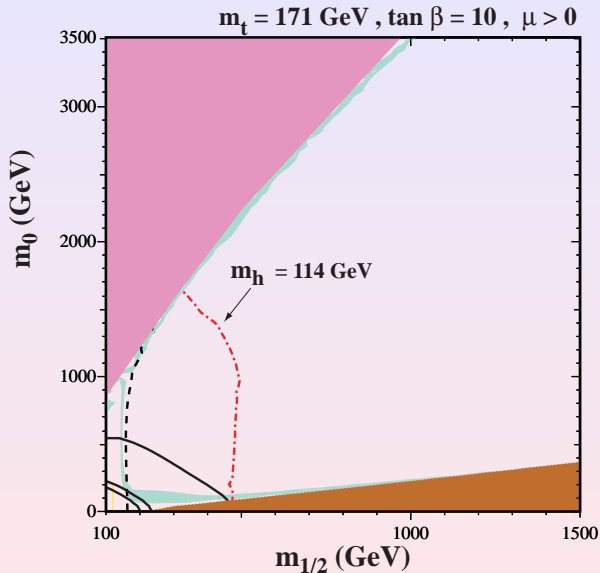
$$\chi = Z_{11}\tilde{B} + Z_{12}\tilde{W} + Z_{13}\tilde{H}_1 + Z_{14}\tilde{H}_2$$

possible **WIMP** candidate

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- or **split supersymmetry**



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- **accelerator searches:**
  - $p_T$  as “easy” signal
  - test couplings, ...
  - probes only short lifetimes

# Non-thermal DM: Axions

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⇒ axions are “like” pions, thus

$$m_a = m_\pi \frac{f_\pi}{f_a} \sim 0.6 \text{eV} \frac{10^7 \text{GeV}}{f_a}$$

i.e. light axions decouple



- coupling to photons

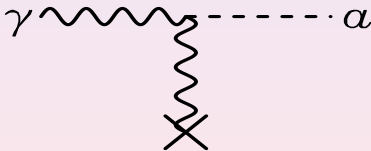
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- Primakoff effect:



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- **axionic strings** form during the PQ phase transition and **emit axions** later on.

# Stellar evolution limits:

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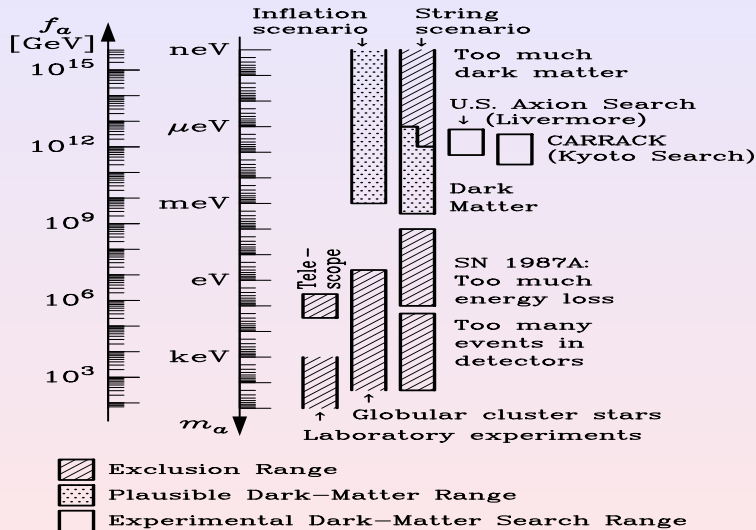
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- self-regulated nuclear burning via interplay of thermal pressure and gravitation
- novel energy loss leaves stellar structure nearly unchanged, but leads to heating and thus to increased consumption of nuclear fuel
- reduction of stellar lifetime:

$$\frac{\delta\tau}{\tau} \sim \frac{L_a}{L_\gamma} \lesssim 1$$

⇒ upper limit on  $g_{\alpha\gamma}$ ,  $m_a$ ; lower limit on  $f_a$

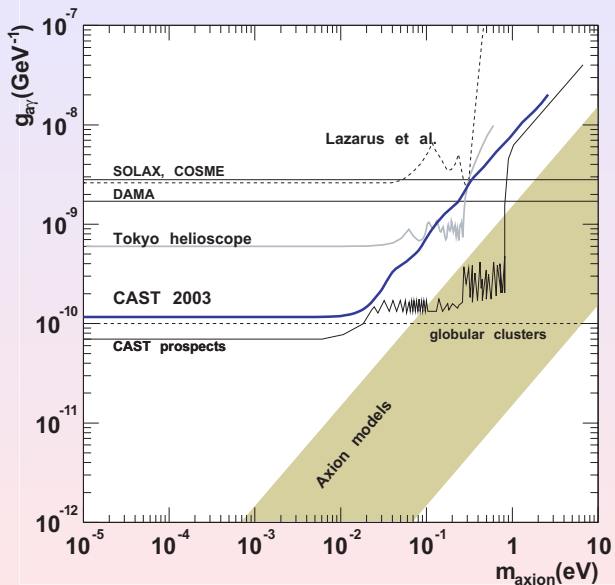
# Summary of (old) axion limits:



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# Superheavy matter

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- In inflationary cosmology

$$\Omega_X h^2 \sim \left( \frac{M_X}{10^{12} \text{GeV}} \right)^2 \frac{T_{RH}}{10^9 \text{GeV}}$$

independent of details of particle physics, for any  $M_X \lesssim H_I$



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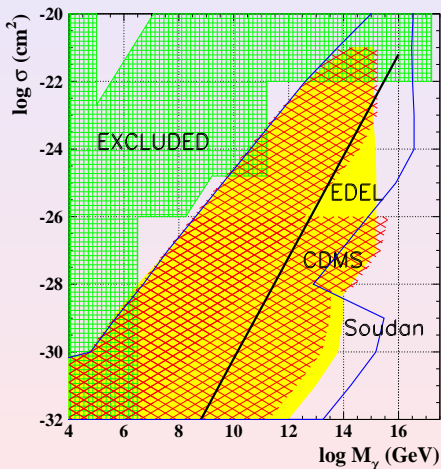
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lifetime:

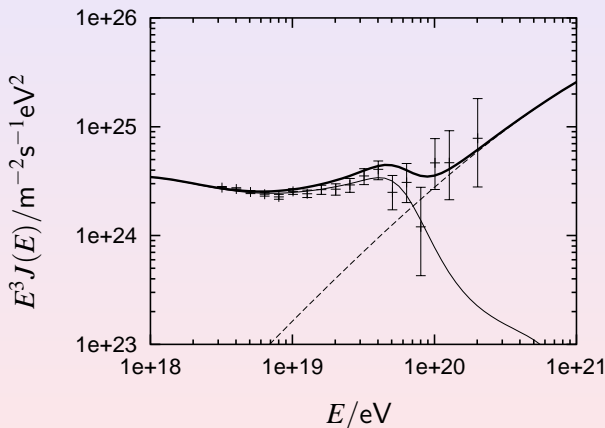
- **metastable**  $\tau \gtrsim T_0$  or
- **stable** due to some (gauged)  $R$  symmetry

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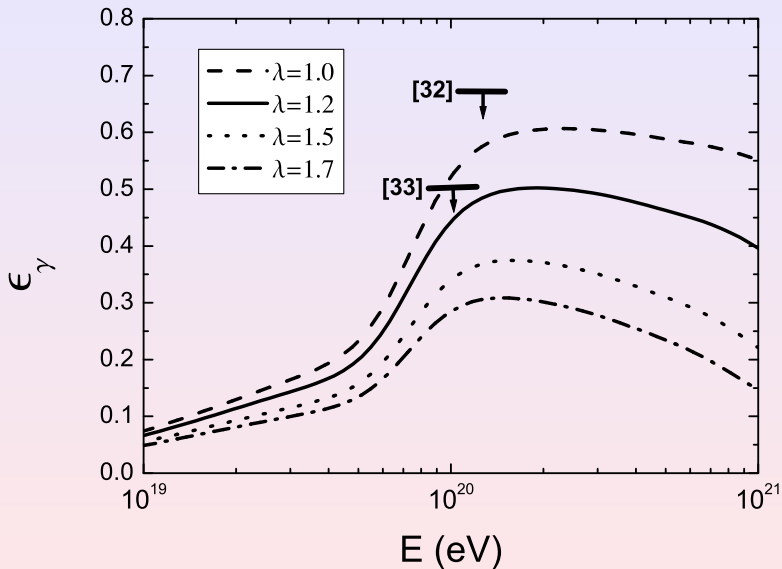
- **direct detection:** density  $1/M_X$ , recoil energy is constant  
 $\Rightarrow$  large  $\sigma_{XN}$  required



- UHECR above the GZK cutoff via photon, nucleon secondaries



# Detection/exclusion of superheavy matter:



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