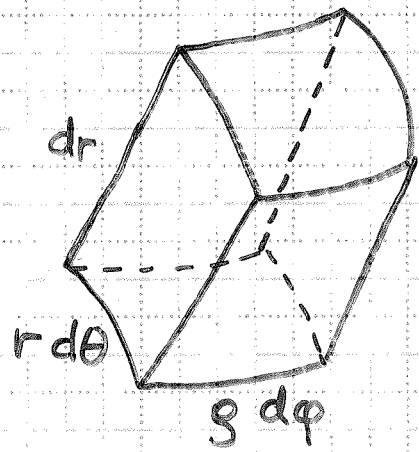
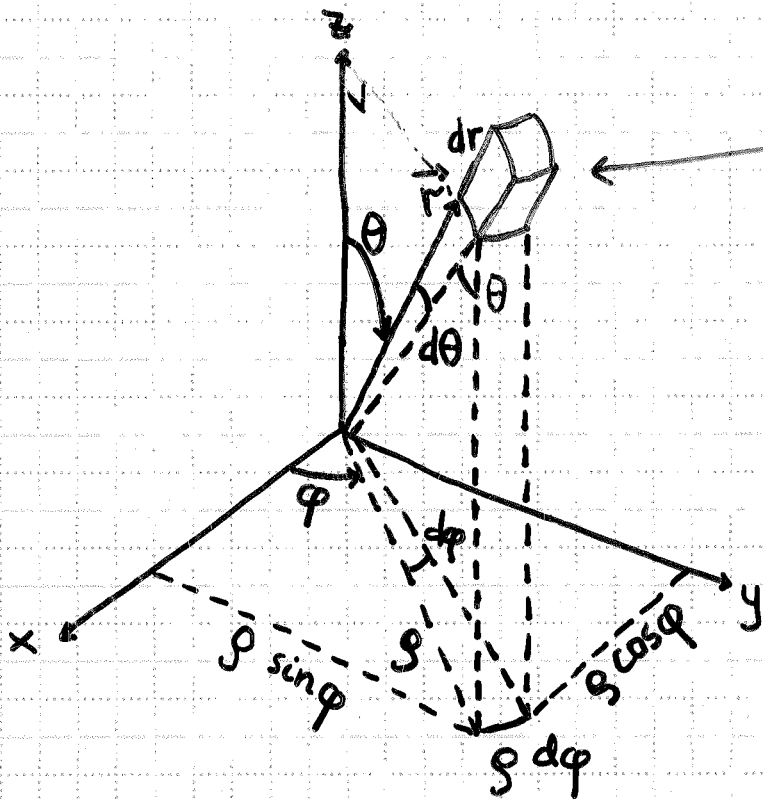


# Volumeelement i kulekoordinater: $(r, \theta, \varphi)$



$$\Rightarrow dV = (dr) \cdot (r d\theta) \cdot (\rho d\varphi)$$

$$\rho = r \sin \theta$$

$$\Rightarrow dV = r^2 dr \sin \theta d\theta d\varphi$$

$$z = r \cos \theta ; \quad y = \rho \sin \varphi = r \sin \theta \sin \varphi ;$$

$$x = \rho \cos \varphi = r \sin \theta \cos \varphi$$

$r$ : avstand fra sentrum (origo),  $r = \sqrt{x^2 + y^2 + z^2}$

$\theta, \varphi$ : retning i rommet (i forhold til  $x, y, z$ )

alle mulige retninger:  $0 \leq \theta \leq \pi$

$$0 \leq \varphi \leq 2\pi$$

Eks:  $\theta = 0 \hat{=} \text{Langs } \hat{z}$

$(\theta = \pi/2, \varphi = 0) \hat{=} \text{Langs } \hat{x}$

$(\theta = \pi/2, \varphi = -\pi/2) \hat{=} \text{Langs } -\hat{y}$