13.3 Quantum corrections to $\langle \phi \rangle$.

Consider the propagator at coincident points,

$$\langle \phi(0)^2 \rangle = \lim_{x \to 0} \int \frac{d^d}{(2\pi)^d} \, \frac{\mathrm{e}^{-\mathrm{i}kx}}{k^2} \,.$$
 (260)

Additionally to the usual UV divergence (which we may cure introducing a simple cutoff), the propagator of a massless field may have an IR divergence: The integral diverges for $k \to 0$, if $d \leq 2$. But $\langle \phi(0)^2 \rangle \to \infty$ means that our classical field is not trapped in a minima. Thus SSB is only possible for d > 2, a result called Coleman–Mermin-Wagner theorem.