

KAP 8: Hamiltons ligninger

- $H = \underbrace{p_i \dot{q}_i - L}_{\text{Legendretransformasjon}} ; H = H(q, p, t) \text{ mens } L = L(q, \dot{q}, t)$
Legendretransformasjon \Rightarrow variabelskifte, fra (q, \dot{q}, t) til (q, p, t)
- Hamiltons ligninger: $\dot{q}_i = \frac{\partial H}{\partial p_i}$ $\dot{p}_i = -\frac{\partial H}{\partial q_i}$ ($\frac{\partial L}{\partial t} = \frac{\partial H}{\partial t}$)
- Sentralfelt: $H(q, p) = \frac{1}{2m} (p_r^2 + p_\theta^2/r^2 + p_\phi^2/r^2 \sin^2 \theta) + V(r)$
- E.m. felt: $H(x_i, p_i, t) = \frac{1}{2m} (\vec{p} - q\vec{A})^2 + q\phi$

KAP 3: Sentralfelt; 2-legemeproblem

- 2 legemer + sentralfelt $V(r) \rightarrow$ ekvivalent 1-legemeproblem:
 $L = T - V = \frac{1}{2} \mu \vec{r}^2 - V(r)$
 red. $\vec{r} \uparrow$ relativkoord.
 masse

\vec{L} bevarst \Rightarrow plan bevegelse: $\vec{r} \rightarrow (r, \theta)$

$$r(t) \text{ gitt ved } t = \int_{r_0}^r \frac{dr}{\sqrt{\frac{2}{m}(E - V - \ell^2/mr^2)}}$$

$$\bullet r(\theta) \quad \theta = \theta_0 + \int_{r_0}^r \frac{dr}{r^2 \sqrt{\frac{2mE}{\ell^2} - \frac{2mV}{\ell^2} - \frac{1}{r^2}}}$$

$$\bullet \text{Kepler-problemet: } V = -k/r \Rightarrow r = \frac{p}{1 + \epsilon \cos \theta} \quad (\text{kjeglesnitt})$$

$$\bullet \text{Spredning i sentralfelt: } r(\theta) \sim 1/\sin^2 \theta/2 \quad (\text{Rutherford})$$

Spredningsstverrsnitt:

$$\sigma(\Omega) d\Omega = \text{antall partikler spredt inn i } d\Omega \text{ pr tidsenhet / innfallende intensitet}$$

$$\Sigma = \int \sigma(\Omega) d\Omega = \text{totalt spredningsnitt}$$