

Stregens løsning: $y(x,t) = \begin{cases} y_i(x,t) + y_r(x,t) & x \leq 0 \\ y_t(x,t) & x \geq 0 \end{cases}$

Må tilfredsstille alle fysiske betingelser til enhver tid.

Kun mulig dersom

$$\omega_i = \omega_r = \omega_t$$

$$\text{og } \varphi_i = \varphi_r = \varphi_t$$

Setter $\omega_i = \omega$ og vælger $\varphi_i = 0$

$$\Rightarrow y_i(x,t) = y_{i0} \sin(k_i x - \omega t)$$

$$y_r(x,t) = y_{r0} \sin(k_i x + \omega t) \quad (v_r = v_i \Rightarrow k_r = \frac{\omega}{v_r} = \frac{\omega}{v_i} = k_i)$$

$$y_t(x,t) = y_{t0} \sin(k_t x - \omega t)$$

$$y \text{ kontinuert i } x=0 \Rightarrow -y_{i0} \sin \omega t + y_{r0} \sin \omega t = y_{t0} \sin \omega t$$

$$\Rightarrow y_{i0} - y_{r0} = y_{t0}$$

$$\partial y / \partial x \text{ kont. i } x=0 \Rightarrow k_i y_{i0} \cos \omega t + k_i y_{r0} \cos \omega t = k_t y_{t0} \cos \omega t$$

(egenlig: $S \cdot \partial y / \partial x$!!)

$$\Rightarrow k_i y_{i0} + k_i y_{r0} = k_t y_{t0}$$

$$\Rightarrow y_{r0} = \frac{k_t - k_i}{k_t + k_i} y_{i0}; \quad y_{t0} = \frac{2k_i}{k_t + k_i} y_{i0}$$

Med $k_i = \omega/v_1$, $k_t = \omega/v_2$, $v_1 = \sqrt{S/\mu_1}$ og $v_2 = \sqrt{S/\mu_2}$:

$$\boxed{y_{r0} = \frac{\sqrt{\mu_2} - \sqrt{\mu_1}}{\sqrt{\mu_2} + \sqrt{\mu_1}} y_{i0}; \quad y_{t0} = \frac{2\sqrt{\mu_1}}{\sqrt{\mu_2} + \sqrt{\mu_1}} y_{i0}}$$