

3 ligninger med 2 ukjente ?? Nei:

Multipliser (a) med $-c/n_2$ på begge sider og bruk

$$E_1 \sin \theta_1 = \frac{1}{v_1^2 \mu_1} \cdot \frac{n_2 \sin \theta_2}{n_1} = \frac{n_1}{v_1 c \mu_1} \cdot \frac{n_2 \sin \theta_2}{n_1} \quad \text{og}$$

$$E_2 \sin \theta_2 = \frac{1}{v_2^2 \mu_2} \sin \theta_2 = \frac{n_2 \sin \theta_2}{v_2 c \mu_2}. \quad \text{Vi ser da at}$$

ligning (a) og (c) gir akkurat det samme, nemlig:

$$E_{ipo} - E_{rpo} = \beta E_{tpo} \quad (\beta \equiv \mu_1 v_1 / \mu_2 v_2)$$

Mens (b) kan skrives slik:

$$E_{ipo} + E_{rpo} = \alpha E_{tpo} \quad (\alpha \equiv \frac{\cos \theta_2}{\cos \theta_1})$$

Løsning:

$$\begin{aligned} E_{rpo} &= \frac{\alpha - \beta}{\alpha + \beta} E_{ipo} \\ E_{tpo} &= \frac{2}{\alpha + \beta} E_{ipo} \end{aligned}$$

$$\alpha = \frac{\cos \theta_2}{\cos \theta_1} = \frac{\sqrt{1 - \sin^2 \theta_2}}{\cos \theta_1} = \frac{\sqrt{1 - n_1^2 \sin^2 \theta_1 / n_2^2}}{\cos \theta_1}$$

$$[\text{Kontroll: } \theta_1 = 0 \Rightarrow \alpha = 1 \Rightarrow E_{rpo} = \frac{1 - \beta}{1 + \beta} E_{ipo}; \text{ OK!}]$$